

**Preparation of Nairobi County Wind Map as Part of the Kenya National  
Annex to En 1991-1-4**

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of Science in Civil Engineering (Structural Option).**

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## DECLARATION

This thesis is my original work and has not been submitted to any other university for examination.

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This thesis has been submitted for examination with our approval as University supervisors.

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## **DEDICATION**

This research is dedicated to my family especially my dear mum who has always believed in me and have always supported me as I strive to achieve my dreams.

## **ABSTRACT**

Structural engineering education and practice in Kenya has been based on British Standards which are developed and maintained by the British Standards Institution (BSI). Given that BSI has decided to change to Structural Euro codes, the way forward for engineering design training and practice is to adopt the use of Euro codes. For Kenyan engineers to switch to the use of Eurocode 1991-1-4 on Wind loads, they need to develop a National Annex to that code to take care of the local wind characteristics. Part of the information to be put in the annex is a wind map that enables evaluation of wind loads by Eurocode 1991-1-4

This research was carried out as an initial step in the development of the Kenyan National Annex (NA) of the EN1991-1-4 by developing a wind map illustrating the basic 50 year return period design wind speeds in Nairobi County. Hourly wind speeds were obtained from the Kenya Meteorology Department and the environmental correction factors (both terrain and altitude correction factors) determined. The combined factors were then multiplied to the hourly wind speeds and the maximum wind speeds from each storm derived. These were then subjected to extreme value analysis to come up with the basic hourly wind speeds which were then multiplied by a factor of 1.06 to get the 10-minute wind speeds from which a wind contour map was drawn. The results show that the 10-minute wind speeds within Nairobi County vary from 18m/s to 22m/s. Currently, a 3-second gust speed of 28m/s is used in the design of structures within Nairobi Country. When converted to the 10-minute wind speed using the gust curve shown in figure 2.1, it resulted to a 10 minute wind speed of 19.63m/s. This is comparable to the 10 minute wind speeds obtained from this research.

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## **CHAPTER 1: INTRODUCTION**

### **1.1 BACKGROUND**

Euro codes are a set of harmonized technical rules developed by the European Committee for Standardization for the structural design of construction works in the European Union. They are expected to replace the existing national building codes published by the European national standard bodies like the British Standard Institution (BSI). Each country is expected to issue a national annex to the eurocodes which will need referencing for a particular country. The implication of this for countries switching to eurocodes is that the national building codes will not be updated in keeping up with new knowledge thus they will be outdated after some time. Structural engineering education and practice in Kenya and in most of the commonwealth countries has been based on British standards which are developed and maintained by the British Standards Institution (BSI). Given that BSI has decided to change to structural euro codes, the way forward for engineering design training and practice is to adopt the use of euro codes. Changing to euro codes will open international construction markets to Kenyan engineers, making competition possible in the fields of studies and construction activities. Switching will also allow keeping up with the evolution of the codes – no longer the case for BS. The attractive features of the euro codes are (Guide to the use of EN 1991-1-4-Wind Actions, 2006):

1. General Part: This part is the same for all participating countries.
2. National Annex: This part allows for development of nationally determined parameters (NDP).

The participating country undertakes definition, conception and publication of national annexes to be used in conjunction with the euro codes.

The national annexes give alternative procedures, values and recommendations for classes with notes indicating where national choice may be made. Therefore the national standard institutions e.g. Kenya Bureau of Standards (KEBS) implementing the euro codes should come up with national annexes to the various euro codes containing nationally determined parameters to be used for the design of buildings and civil engineering works to be constructed in the relevant country.

In the case of EN 1991-1-4, there are various parameters that need to be determined for each country before it can be implemented. One of the most important parameters that should be determined is the fundamental basic wind speed that will be contained in a national wind map. This fundamental basic wind velocity is a key parameter in the determination of wind loads for the design of structures. The fundamental basic wind velocity is the mean wind velocity for a 10 minute averaging period with an annual risk of being exceeded of 0.02, at a height of 10m above ground level at an area with low vegetation such as grass and isolated obstacles (trees, buildings) with separations of at least 20 obstacle heights ( $Z_0 = 0.05\text{m}$ ) (Guide to the use EN 1991-1-4-Wind Actions, 2006)7.

Kenyan structural engineers currently use two documents for the determination of wind loads for the structural design of buildings i.e. CP 3: Chapter V: Part 2 and BS 6399 Part 2. Both of these documents were prepared by United Kingdom. However, CP 3: Chapter V: Part 2 uses a 3 second gust wind speed while BS 6399 Part 2 uses a mean hourly wind speed in the determination of wind loads on structures. The Kenyan wind map that shows the basic wind speeds was developed in the 1970s. This map was developed using the 3 second gust speed and has never been updated since then. Moreover, there is no document showing how the wind speeds were determined. Old structural engineers in the country say that the wind speeds were determined by British engineers based on the similarity between the wind speeds

indifferent areas in Kenya and those recorded in the United Kingdom. The wind speeds for the different regions that are currently in use in Kenya are as follows:

**Table 1.1: Different regions and their wind speeds in Kenya.**

REGION	WIND SPEED IN M/S
Nairobi, Central and Southern Half of Eastern Province	28
Northern Half of Eastern and North Eastern Province	40
Coast Province	31
Southern Part of Rift Valley	36
Nyanza and Western Province	46

The fundamental basic wind speeds to be contained in the EN 1991-1-4 wind map are set to be different from the ones currently in use in Kenya due to the following reasons:

- The fundamental basic wind speeds in the EN 1991-1-4 wind map are based on a 10-minute mean velocity while the wind speeds currently in use were based on a 3 second gust speed.
- The fundamental basic wind speed to be used in EN 1991-1-4 are based on a reference terrain roughness which is an area with low vegetation such as grass and isolated obstacles (trees, building) with separations of at least 20 obstacle heights while the wind speeds currently in use have a reference terrain of an open situation.

Due to these differences the wind map to be used in EN 1991-1-4 is set to have different wind speeds from the ones currently in use. It is also important that Kenya develops its own wind map containing scientifically determined fundamental basic wind speeds that can be used in

determination of wind loads. This will also take care of the climatic changes that have taken place in the country from the time the wind speeds currently in use were determined.

This research was carried out as an initial step in the development of the Kenyan National Annex (NA) to the EN1991-1-4 by coming up with a wind map illustrating the basic 50 year return period design wind speeds in Nairobi County. This wind map was based on historical wind records across Nairobi County and detailed the 10-min mean wind speed at an area with low vegetation such as grass and isolated obstacles (trees, building) with separations of at least 20 obstacle heights ( $Z_0 = 0.05\text{m}$ ) which had a probability of 0.02 of being equalled or exceeded in any one year. The map wind speed was adjusted using an altitude factor given in the United Kingdom (UK) National Annex.

## 1.2 Research Problem.

Kenyan structural engineers have been using the British Standards for structural design. However, the British standards are being phased out to give way to euro codes. The way forward is to switch to the euro codes. In the determination of wind loads on buildings as per EN 1991-1-4, the following steps are followed:

1. Read  $V_{b,0}$  from map

$$2. V_b = C_{dir} \cdot C_{season} \cdot C_{prob} \cdot V_{b,0} \dots \dots \dots \text{Equation 1}$$

$$3. q_b = \frac{1}{2\rho V_b^2} \dots \dots \dots \text{Equation 2}$$

$$4. q_b = C_e(z)q_b \dots \dots \dots \text{Equation 3}$$

$$5. W_e = q_b(z)C_{pe} \dots \dots \dots \text{Equation 4}$$

$$6. F_w = C_s C_d \sum W A_{ref} \dots \dots \dots \text{Equation 5}$$

Where:

$V_{b,0}$  = The fundamental basic wind speed that can be read directly from the wind map

$V_b$  = The fundamental basic wind velocity modified to account for seasonal and directional factors

$C_{dir}$  = The direction factor used to modify the basic wind speed to produce wind speeds with the same risk of being exceeded in any wind direction

$C_{season}$  = The season factor used to modify the basic wind speeds with the same risk of being exceeded in any specific sub-annual period

$C_{prob}$  = The probability factor used to modify the basic wind speed to change the risk of wind speed being exceeded.

$Q_b$  = The basic velocity pressure derived from the basic wind velocity ( $q_b = 0.613 V_b^2$ )

$C_s C_d$  = The structural factor that takes account of the effect of non-simultaneous wind action over the surfaces of the structure

$C_e(z)$  = The exposure factor that accounts for the effect of terrain, orography and building height.

$W_e$  = The wind pressure acting on external building surface.

$C_{pe}$  = External pressure coefficient which is the ratio of pressure acting on the external surface to the peak velocity pressure.

$F_w$  = The wind force acting on the overall structure or element

From the above equations used in the determination of wind loads, the basic wind speed is a key parameter in determining the wind loading on a structure at a particular location.

Therefore for Kenyan engineers to switch to the use of EN 1991-1-4 on wind loads, it is necessary to come up with a wind map containing the fundamental basic wind speeds in different localities so that the wind loads can be determined. This will enable engineers to

carry out safe and economical design of structures especially high rise structures whose design is significantly affected by wind loads.

### **1.3 OBJECTIVES**

#### **1.3.1 General Objective**

To prepare a wind map of Nairobi County to be part of the Kenyan National Annex to Eurocode 1991-1-4.

#### **1.3.2 Specific Objectives**

1. To determine altitude correction factors in Nairobi County.
2. To determine terrain correction factors in Nairobi County.
3. To determine the 10 minute mean wind velocity with an return period of 50 years

## **CHAPTER 2: LITERATURE REVIEW**

### **2.1 Wind Action**

Wind is defined as air in motion. It can be in any direction though in most cases the horizontal component is greater than the vertical component. It develops due to spatial differences in the atmospheric pressure. These differences are due to uneven absorption of solar radiation on the earth's surface. Wind is mainly influenced by the earth's rotation (Coriolis forces) and frictional forces especially near the earth's surface.

Wind causes pressure at points on objects in its path. The wind kinetic energy has a potential pressure called the dynamic pressure that is proportional to the square of the wind speed. This potential pressure acts at points where the objects stop the wind therefore the pressure distribution causes forces to act on the objects. Wind engineering analyses wind effects on the natural and built environment. Structural engineers focus on strong winds which can cause damage. Since structures are becoming taller and more slender, the effect of wind is becoming critical.

### **2.2 Wind Climate in Nairobi County.**

The City of Nairobi is located between 36 50' E mid 1 18'S. The mean altitude is about 1700 metres above the mean sea level but since the city has a highly variable topography, this height ranges from 1600m (to the east) to over 1800m (to the west and northwest of the central business district (CBD).The prevailing winds are mainly in the easterly direction.

North-easterly winds prevail during the northern winter while south-easterlies are dominant during the southern winter. Computed frequency roses have shown that the surface winds at the city of Nairobi have a high frequency of easterly flow for the whole year. However, some westerlies are observed during the period June, July and August which are associated with the high pressure ridge that prevails over East Africa during the period. During this period, the

winds are also observed to be more variable both in speed and direction. There is also large diurnal variability with the day-time winds being highly constant in direction than is the case with night-time conditions. (Ng'ang'a, 1992).

## **2.3 Wind Loads.**

Wind loads need to be considered in the design of structures. This is especially so for high-rise and light weight structures. Since wind loads are usually specified as pressure due to the predicted maximum wind velocity, it is important to predict a maximum wind velocity that can be expected over the design life of structures so that the design is carried out with these wind speeds in mind. Wind loading standards provide procedures for determining the loads on specific structures in specific locations for specific conditions and needs. They start with general (neutral) conditions and move towards the specific conditions.

### **2.3.1 Basic Wind Speed**

The basic wind speed is defined as the maximum expected wind speed at the standard height above the ground on a reference terrain over a chosen recurrence interval. This speed is established by extreme value analysis of the wind data collected from meteorological stations in a given geographical region over a period of time. (Celik, 2004, Bivona et al., 2003, Coelingh et al., 1996). The wind speeds for different regions are usually used to draw a wind speed map. The basic wind speed used in the determination of the wind load on a structure in a given location is read from this wind speed map.

EN 1991-1-4, (2005) defines the basic wind velocity as the characteristic 10 minutes mean wind velocity, irrespective of wind direction and time of year, at 10 m above ground level in open country terrain with low vegetation such as grass and isolated obstacles with separations of at least 20 obstacle heights. BS 6399-2, (1997) on the other hand defines the basic wind speed as the hourly mean wind speed with an annual risk  $Q$  of being exceeded of 0.02,

(Return period of 50 years) irrespective of wind direction, at a height of 10 metres over completely flat terrain at sea level that would occur if the roughness of the terrain was uniform everywhere (including urban areas, inland lakes and the sea) and equivalent to typical open country in the United Kingdom. CP3: Chapter V: Part 2, (1972) defines the basic wind speed as the 3-second gust speed, at 10m above ground in an open situation that is likely to be exceeded on average only once in 50 years.

In the OAS/NCST/BAPE Code of Practice for Wind Loads for Structural Design, (1981) the basic wind speed is defined as the 3-second gust speed estimated to be exceeded averagely only once in 50 years at a height of 10m above the ground in an open situation. This speed is adjusted for specific cases using various parameters including averaging period, return period, ground roughness, height, topography and size of the structure in order to obtain the design wind speed for the particular cases. However, there are cases such as CUBiC, (2012) where the apparent starting point for computation is the basic wind pressure. In this case the basic wind pressure has been predetermined by the building code from the basic wind speed. The way in which standards progress from basic wind speeds to design wind speeds differ from one standard to the other. However all other things being equal, the end results should be the same which is the design wind speed.

From the definitions of basic wind speeds given in the above mentioned building codes, in coming up with basic wind speeds map, the following parameters or methodologies need to be defined: the method to be used for extreme value analysis of the wind speeds, the averaging period, the standard reference terrain, the standard height, the probability of recurrence and the method used to map the basic wind speeds.

### **2.3.2 Extreme Value Analysis of Wind Speeds**

Wind speed is a random variable which is affected by a lot of factors such as geometric shapes, roughness, and elevations of ground surface. Therefore, the easiest and most direct means of obtaining wind speed distribution in different locations is to set up a measurement station at each location. The wind speed of short recording time is usually higher than the wind speed of long recording time. Those extreme values obtained from observed data are considerably important to engineering applications. The maximum wind pressure, i.e. extreme-value wind speed, is the major variable to be considered for structural wind resistant design.

A major question that arises in the wind speed extreme value analysis is the type of probability distribution that is best suited for modelling the behaviour of extreme winds. Since wind speed is a probabilistic event, researchers have extensively studied the probability distribution function that better fit the extreme value of wind speed. Type I extreme value distribution is widely used to evaluate the design wind speed values. (Coelingh,1996).

Thom, (1960) has studied the annual extreme wind data for 141 open country stations in the United States of America (USA). Type II Extreme Value distribution was chosen to fit the annual extreme wind series to give isotachs maps for 2, 50 and 100-year mean recurrence intervals. Thom, (1968) has also developed new distributions of extreme winds in the USA for 138 stations. New maps were drawn for 2-year, 10-year, 25-year, 50-year and 100-year mean recurrence intervals. In carrying out his study, he used the Type II (Frechet) distribution. He indicated that examination of extensive non-extreme wind data showed that such data follow a log-normal distribution quite closely, which reinforces his choice of Type II distribution. Simiu et al (1975) presented a study in which a 37 year series of five minute largest yearly speeds measured at stations with good climates were subjected to the probability plot correlation coefficient test to determine the tail length parameter of the best

fitting distribution of the largest values. Of the series, 72% were best modelled by Type I distribution or equivalently by the Type II distribution with  $y=13$ ; 11% by the Type II distribution with  $7 < y < 13$ ; and 17% by the Type II distribution with  $2 < y < 7$ . Simiu and Scalan, (1986) also obtained the same percentages from the analysis of 37 data sets generated by Monte-Carlo simulation from a population with a Type I distribution which indicates that in a well-behaved climate extreme wind speeds are better modelled by Type I rather than Type II distributions. Further, Simiu and Filliben, (1976) showed that Type I distribution of the largest values gives an adequate representation of extreme wind behaviour in most regions not subjected to hurricane force winds. For hurricane-prone regions he indicated that type II distribution with a small value of tail length parameter could give a better estimation of extreme wind speeds.

The ANSI A58.1-821 wind load provision is based on a wind speed contour map that was developed by Simiu et al. (1979). The wind speeds in the map were established from the data collected at 129 meteorological stations in the USA. The analysis was done using Type I (Gumbel) distribution. He used data only for locations for which a minimum of 10 years of continuous records were available. The provisions of the National Building Code of Canada are also based on the assumption that the extreme wind speed is best modelled by the Type I distribution. From the studies carried out, it is evident that Type I (Gumbel) distribution is best suited for extreme value analysis in a hurricane free zone like Nairobi County, thus was used in this research.

### **2.3.3 Errors in Prediction of Wind Speeds**

Errors are inherent in the process of wind speed prediction. Besides the errors associated with the quality of the data, there are sampling and modelling errors. The sampling errors are a consequence of the limited size of samples from which the distribution parameters are

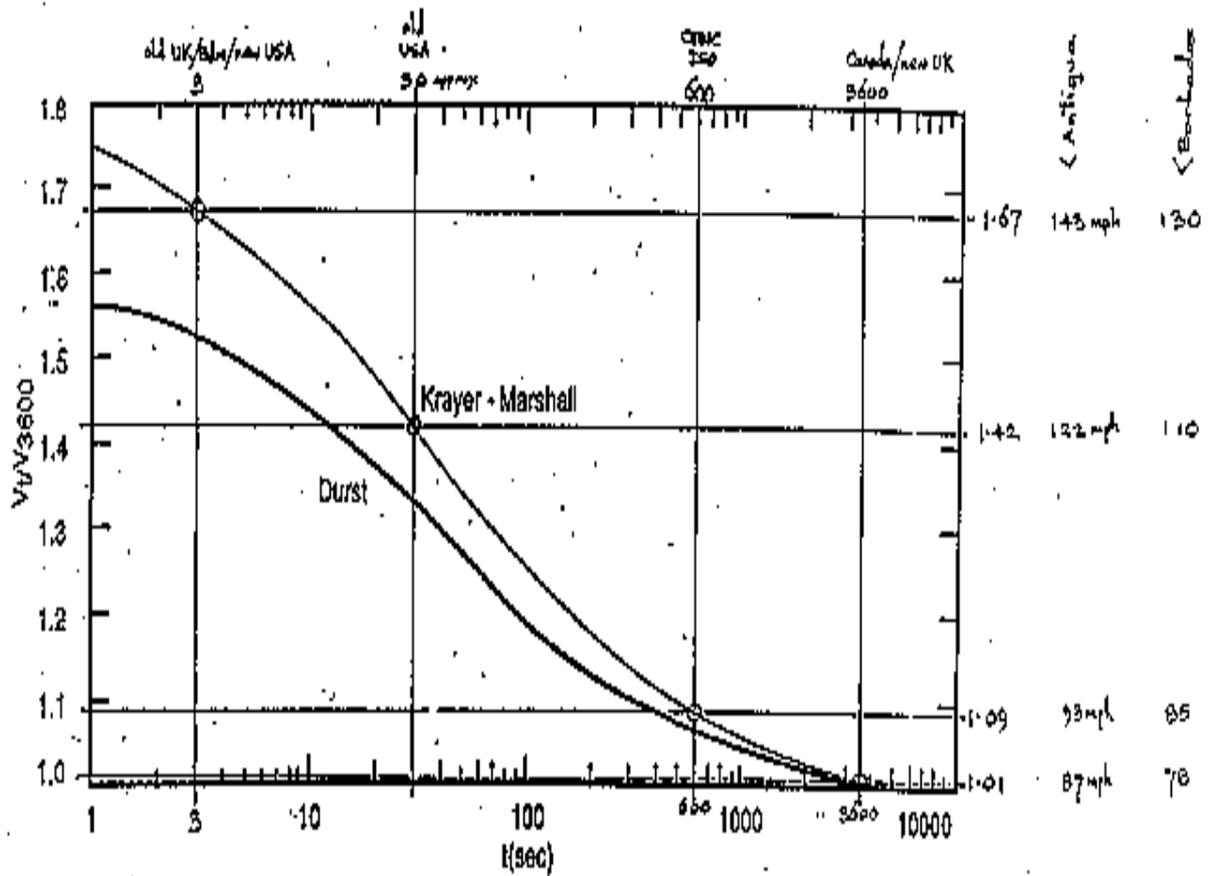
estimated. These errors in theory vanish as the size of the sample increases infinitely (Simiu et al., 1978).

The modelling errors are due to inadequate choice of the probabilistic model. Chi-square and K-S Test are usually performed to choose the best fitting model.

#### **2.3.4 Averaging Period**

Wind speeds are measured by the use of anemometers. These instruments vary in the way they sample the wind and in the way they report the results. One significant characteristic of mechanical anemometers is the response time. This is a function of the inertia of the system. The shortest response time for mechanical anemometers is 1-3 seconds. Many countries have adopted the 3-second gust as the averaging period for the basic wind speed. These countries include Australia, the USA (post 1995) and Barbados. The United Kingdom (UK) used the 3-second gust up to 1995 when they changed to the mean hourly wind speed.

Data averaged over relatively short intervals like 5 second average, can at times be affected by stronger than usual local turbulence, thus resulting in a distorted picture of the mean winds. Averaging over relatively long periods like 10 minutes is therefore desirable. Wind speed measured for any averaging period may be converted to another averaging period using relationships that have been determined experimentally and analytically. During the 1990s Krayner and Marshall (1992) proposed an adjusted S curve for tropical cyclone regions. The Durst curve is used for both tropical and extra-tropical cyclones. Figure 2.1 shows the Durst curve (Ratio of Probable Maximum Speed Averaged over  $t$  seconds to Hourly Mean Speed) which has been in use since the 1960s.



**Ratio of Probable Maximum Speed Averaged over t Seconds to Hourly Mean Speed**

Source: Ref. 4

**Figure 2.1. Ratio of Probable Maximum Speed Averaged over t seconds to Hourly Mean Speed**

EN 1991-1-4 has adopted the use of 10 minutes as the averaging period. However, the wind speed data available in Kenya is in form of mean hourly wind speeds and mean daily wind speeds. Therefore the basic hourly wind speeds have to be converted to 10 minute wind speeds so as to be used in the EN 1991-1-4 to determine wind loads. From Figure 2.1, to convert the wind speeds from a mean hourly averaging time period to a 10-minute averaging time period, the mean hourly basic wind speeds should be multiplied by a factor of 1.06 as shown in equation 6 below.

$$V_{10min} = 1.06 * V_{hourly} \dots\dots\dots \text{Equation 6}$$

### 2.3.5 Return Period

Wind speeds are amenable to statistical analysis. It can be argued that historical records are not long enough for such analyses to be reliable. However, statistical analyses of historical information are usually adjusted on theoretical bases so that they can be used in determining the relative wind speeds expected to occur over different periods of time. A short return period (2 years) is usually recommended for temporary structure and for (incomplete) structures during erection.

Generally, the longer the return period chosen and the lower the probability level chosen, the more conservative will be the design wind speed. Most buildings in Nairobi County are designed for a 50 year design life. Therefore it is appropriate to determine wind speeds with a return period of 50 years. This ensures that there is a very low likelihood of the structure experiencing a higher wind load than the one determined at the design stage during its design life. The mathematical model used to determine the extreme wind speeds for a given return period, R, for a Gumbel distribution is:

$$G\left(\frac{1}{1 - \frac{1}{R}}\right) \dots \dots \dots \text{Equation 7}$$

Where G is the percent point (or the inverse cumulative distribution) function of the Gumbel distribution.

The Gumbel percent point function is:

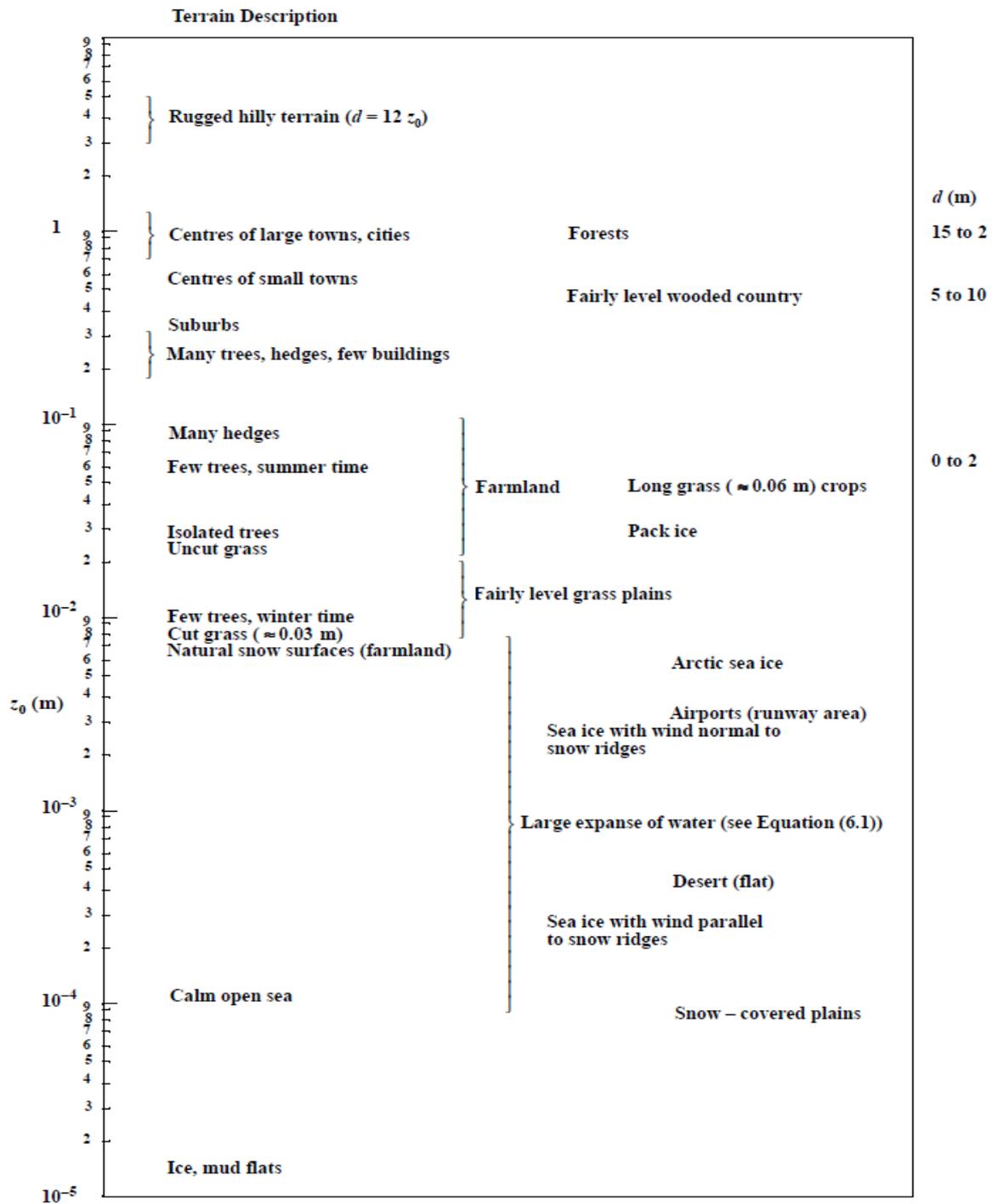
$$-\ln\left(-\ln\left(\frac{1}{p}\right)\right) \dots \dots \dots \text{Equation 8}$$



$$\ln z = V_z(1/2.5u_*) + \ln z_0 \dots \dots \dots \text{Equation 10}$$

Therefore if measured values of  $V_z$  (for heights less than 30m) are plotted against  $\ln z$  for a given site a straight line fit to the data will give a value of  $\ln Z_0$  as the intercept on the  $\ln z$  axis.

**Table 2.1 Values of Surface Roughness Parameter,  $Z_0$**



### 2.3.6 Standard Height

Ground roughness is usually combined with height above ground in wind-loading standards. Height of 10m above ground is considered to be the standard instrument height. Wind data measured at any other height should be adjusted to the standard height by wind profile power law (Masters, 2010). The wind profile power law gives the relationship between the wind speeds at a given height and those at another height. The power law is used where data at various heights must be adjusted to a standard height prior to use. The wind profile of the atmospheric boundary layer (ground surface to around 2000m above ground) is logarithmic and can be best approximated using the log wind profile equation that accounts for parameters like surface roughness and atmospheric stability. However, the wind profile power law relationship often substitutes the log wind profile when surface roughness or stability information is not available. The wind profile power law relationship is:

$$\frac{u}{u_r} = (z/z_r)^\alpha \dots\dots\dots \text{Equation 11}$$

When estimating the wind speed at a certain height  $x$ , Equation 11 is rearranged as follows:

$$u_x = u_r \left( \frac{z_x}{z_r} \right)^\alpha \dots\dots\dots \text{Equation 12}$$

Where:

$U$  is the wind speed in m/s at a height  $z$  in metres

$U_r$  is the known wind speed at a reference height.

$\alpha$  is an empirically derived coefficient that varies dependent upon the stability of the atmosphere. For neutral stability conditions,  $\alpha$  is approximately 1/7.

### **2.3.7 Isotach Map**

Isotachs are lines of equal wind speed on a graph or a chart. An isotachs map is map showing isotachs in a given area. Isotachs are produced from values of basic wind speeds of the various meteorological stations within and around the area. Isotachs can be drawn using various software e.g. ARCGIS, NOVAPOINT, CIVIL 3D etc. These softwares use the following parameters to draw the isotachs: basic wind speeds, grid points (latitude and longitudes) of the meteorological stations. A good contour interval is chosen based on the difference between the highest wind speed and the lowest wind speed. If the difference is small, then a small contour interval e.g. 1 m/s should be chosen while for a big difference in wind speeds, a bigger contour interval e.g. 5 m/s should be adopted so as to give a good contour map. Once the basic wind speeds and the survey grid points (Latitudes and longitudes) have been input into the software and the operator has given a command to generate contours, the software will generate a triangle model in a process called triangulation. Generating a triangle model is a function that positions triangles between individual points and any break line. These triangles are defined by a mathematical process, by which the smallest triangle between three points is found. In a triangulation model, the surveyed points are bound together in a network of triangles. From the triangulation model, the software uses a mathematical process known as interpolation to come up with the basic wind speeds of points within and along the triangles. From these values, the software generates isotachs by connecting points of equal wind speeds.

## 2.4 CASE STUDIES

### 2.4.1 Basis for Wind Map in BS 6399-2

#### a) Derivation of Extreme Wind Information

Wind data, kept by the meteorological office of United Kingdom, were obtained from continuously recording anemographs, exposed at 10m height above the ground in an open, level terrain or, in other terrains, at a height equivalent to the standard exposure. The network of meteorological stations was comprised of about 130 stations and the data kept comprised of hourly mean wind speeds and wind directions, and the details of the maximum gust each hour.

In preparing the basic wind speed map the method used was one that involved the maximum wind speed during each storm. This approach increased the amount of data available for analysis and enabled the directional and seasonal characteristics of the UK wind climate to be examined. A storm was defined as a period of at least 10 consecutive hours with the mean wind speed greater than 5m/s. These periods were identified for 50 anemograph stations, evenly distributed over the UK (mostly having standard exposures), using their records during the period 1970 to 1980. The average number of storms each year was about 140 at most of these stations. For each storm, the maximum hourly mean wind speed blowing from each of the twelve 30<sup>0</sup> wind direction sectors was calculated. The extreme information needed was:

- An improved map of basic wind speeds
- Direction factors
- Seasonal factors.

Extreme wind speeds were analysed in terms of their probability of occurrence whose standard measure is the cumulative distribution function (CDF), given by the symbol P and

corresponding to the annual risk of not being exceeded. Design to resist extreme wind was based on the annual risk (probability)  $Q$  that the hourly mean wind speed will be exceeded given by  $Q=1-P$ . The reciprocal of this is known as the return period. It is the mean interval between recurrences when averaged over a long period. This definition becomes invalid for periods less than 10 years. This concept of return period is not very useful and is open to misinterpretation since the period between individual recurrences varies considerably from this mean value. The concept of annual risk being less open to misinterpretation should be seen as the risk of exceeding the design wind speed in each year the structure is exposed to the wind.

**b) Storm Maxima**

The basic wind speed is estimated to have a risk of  $Q= 0.02$  of being exceeded in a given year. Obtaining this speed for every station requires that all the maximum wind speeds in storms be first abstracted, irrespective of direction. The cumulative distribution function  $P$  that represents the risk of a specific value not being exceeded was determined by the method of order statistics. (BS 6399-2)

In this method the maxima are sorted into ascending order of value and assigned a rank  $m$  ( $m=1$  for the lowest value and  $m=N$  for the highest value), then  $P$  is estimated for the storm maxima by:  $P(v_s) = \frac{m}{N+1}$  ..... *Equation 13*

**c) Annual Maxima**

Maxima from different storms can be regarded as statistically independent, so the CDF  $P_{(v)}$  of annual maximum wind speeds is found from  $P_{(v)} = Pr_{(v_s)}$  where  $r$  is the average annual rate of storms. The CDF of annual maxima is fitted to a Fisher-Tippet Type 1 distribution, defined by:

$$P(v) = e^{-e^{-y}} \dots \dots \dots \text{Equation 14}$$

Where:  $y = a (v-U)$

U is the mode,  $1/a$  is the dispersion.

Therefore:

$$y = -\ln \left[ -\ln \left\{ \left( \frac{m}{N+1} \right)^r \right\} \right] \dots \dots \dots \text{Equation 15}$$

And a plot of  $y$  versus  $V$  (maxima wind speeds) leads to estimates of the annual mode and dispersion. The wind speed  $V$  associated with a specific annual cumulative risk  $P$  of non-exceedance may be found from:

$$V = \left( U + \frac{\ln \left[ \frac{1}{p} \right]}{a} \right) \dots \dots \dots \text{Equation 16}$$

**d) Best Extreme Model**

To obtain the dynamic pressure  $q$ , the maximum wind speed in each storm is multiplied by its square and this is multiplied by half the density of air. Extreme value theory predicts that the Fisher-Tippet Type 1 distribution should be a better fit to dynamic pressure than to wind speed.

This analysis method was repeated for every station using  $q$  as the variable. Results showed that the rate of convergence of storm maxima to the FT1 Model was quicker for the  $q$  model than the  $V_s$  model. The wind speed corresponding to the dynamic pressure having a risk of  $Q=0.02$  of being exceeded at least once a year was used to derive the value for each station.

After that terrain and topographic corrections are made to individual station estimates to ensure that when all the values were plotted on a map, they represented a height of 10m above ground in open, level terrain at mean sea level. Finally isotachs were drawn to be a best fit to the wind speeds plotted.

#### **2.4.2 Basis for Wind Map in Irish National Annex to EN 1991-1-4**

##### **a) Weather Station Auditing**

Analysis of daily maximum gust speeds and hourly maximum speeds for period up to and including 2005 were carried out using extreme value analysis. In addition pictorial documents and historical auditing reports were accessed from Met-Eirean data archives for all the weather stations.

This information was used to evaluate:

- Changes in surroundings over time
- Changes to anemometer location
- Changes to anemometer height and type

The general procedure adopted for analysis of the hourly-mean and daily-gust wind speeds from each anemometer to derive the design wind speeds was as follows:

- I. **Data Quality:** Checking the quality of measurements from each anemometer and separating inconsistent data.
- II. **Exposure Correction:** Transposing wind records from each anemometer (with respect to elevation, topographic and terrain correction) so as to be consistent with open country terrain (Engineering Sciences Data Unit (ESDU))  $Z_0 = 0.03\text{m}$
- III. **Extreme Value Analysis:** Perform an extreme value analysis and assessing directionality using discrete wind records.

IV. **Design Wind Speed Map:** Carrying out a review of the predicted gust and mean wind design for each anemometer and generating contours that account for local topography.

**b) Weather Stations**

Wind records consisting of hourly mean wind speeds and daily gust speeds were analysed over a range of ten to sixty years. The anemometer effective height was taken as 10m. The standard instrument of measurement up to the 1990s was the Dine pressure tube anemometer before being replaced by the Vaisala or Vector rotating-cup anemometer. A trial separation of the gust and mean wind speeds by anemometer type showed small variations and thus the gust and mean data records were separated and independent analysis carried out based on the anemometer type.

**c) Exposure Correction.**

Wind records were corrected for topography, terrain and altitude. These correction factors were assessed for each anemometer and the factors applied to the wind records to get the design wind speeds.

**d) Terrain Assessments**

The atmospheric boundary layer model used in the ESDU analyses was that developed by Deaves and Harris. It takes account of varying surface roughness with fetch. Surface roughness length is characterised by a typical  $Z_0$ , in line with the model used in ESDU. In this method the varying terrain roughness with fetch at  $30^0$  sectors about the origin is taken account of. A detailed survey of the terrain roughness was carried out for each anemometer using methods such as aerial topography, OSI Trail Master and satellite imagery.

The analysis was carried out for each of the twelve  $30^0$  sectors of wind direction to a distance in excess of 40 km from the anemometer and for each sector and patch of the terrain, a



$$P_v = 1 - \exp\left[-\left(\frac{V}{C}\right)^k\right] \dots \dots \dots \text{Equation 18}$$

Where ‘c’ and ‘k’ are empirical constants for a best fit to individual data sets.

Pv is the probability that a velocity will be less than a velocity V.

Theoretically, for a set of data conforming to a Weibull distribution, the CDF of the extremes will converge towards a Fisher-Tippet Type I distribution which is of the form:

$$P_x = \exp[-\exp(-y)] \dots \dots \dots \text{Equation 19}$$

Reduced variate y, is given by the following equation:

$$y = -\ln[-\ln(P_x)] \dots \dots \dots \text{Equation 20}$$

PX is the probability that an extreme value will be less than a value x in any given year.

The extreme value is equated to the square of the wind velocity to ensure a rapid convergence to the extreme value distribution. The two methods of extreme value analysis carried out in an assessment were: a modified Gumbel analysis (annual maximum data) and a Harris Independent Storms (using the maximum ‘2.4 x years of data’ wind speeds from independent storms). These methods are valid for both daily gust and hourly mean wind speeds. The design wind speeds that resulted from the two methods of analysis were compared for consistency.

**h) Analysis of Annual Maxima Data**

The following procedure was used for fitting recorded annual maxima to the Type 1 Extreme Value distribution.

- Extract the largest wind speed in each calendar year of the wind record.
- Rank the series in order of smallest to largest.



Thus the smaller values of pairs of wind records separated by 3 days or less were deleted to ensure only independent storm maxima were retained. With the exception of the calculation of the reduced variate, the procedure for analyzing the independent storm data is similar to that for the yearly maxima.

The probability that the extreme value will not be exceeded in any given year is based on the rank of the wind speed when compared to the total number of storms usually taken as 2.4 x years of data. The plotting positions are modified based on probability weighted least squares. This probability analysis provides design speeds for various return periods, with greater confidence associated with shorter return period events.

#### **j) Errors in Analysis**

There is an amount of uncertainty in the estimation and the precision of design wind speed estimates when using the methods of analysis outlined above. The estimates depend on both the length and quality of the wind records. There are cases where the recorded wind maxima fall outside confidence limits. Common reasons that account for obscure wind records include:

- The value may originate from a storm with a different mechanism.
- The event may have a smaller probability of occurrence than the analysis indicates due to the finite record length not containing other intermediate storm events which would eventually occur.
- The value could be due to a manual/rounding error.

#### **k) Mean and Gust Wind Speeds**

The use of mean speeds over gust speeds has been favoured due to the theoretical stability of measurement of mean speeds and the problems experienced when interpreting and comparing gust speed records from different anemometer and recording systems. Statistical variation and

random measurement problems lead to over-prediction of extremes. However, gust speeds are much less sensitive to changes of terrain roughness and site exposure and the prediction reliability is of less concern with long data records.

### **l) Directionality of Design Winds**

Direction factors are applied to site specific design wind speed so that designers can carry out a more accurate assessment of the wind loading of a structure. Non-inclusion of direction factors in a design assessment could easily lead to over-design. Direction factors were derived by dividing every independent directional design wind speed by the maximum directional design wind speed.

### **m) Design Wind Map for Ireland**

The mean hourly directional wind speeds from all the anemometers were converted into 10-minute mean wind speeds using a 1.06 conversion factor which has also been used in generating the wind map of the UK National Annex. The average gust factor based on 50-year wind speed predictions is calculated and a more conservative value is used to convert the design gust speeds to hourly mean design speeds. The 10-minute mean design speeds were plotted on the map of Ireland and contour lines drawn to fit. (Derivation of Irish Wind map, 2009).

## CHAPTER 3: METHODOLOGY

### 3.0 General procedure

The general procedure that was adopted for collection and analysis of the hourly-mean wind speeds from each of the anemometers to derive design wind speeds was as follows;

- **Data Collection and Quality Check:** The data was collected and a check done on the quality of measurements for each anemometer. Inconsistent data records were removed from the data set.
- **Exposure Correction:** Wind records from each anemometer were transposed (considering elevation and terrain corrections) to be consistent with open country terrain.
- **Extreme Value Analysis:** Extreme value statistical analysis was carried out using discrete wind records.
- **Design Wind Speed Map:** The predicted mean wind speeds for each anemometer were used to generate a wind map.

### 3.1 Data Collection and Quality Check.

Hourly mean speeds and wind direction data that were available at all the meteorological stations within and immediately around Nairobi County were collected from Kenya Meteorological Department (KMD). The meteorological stations from which data was obtained were: Dagoretti, Wilson Airport, JKIA, Eastleigh Airbase, Kabete, Machakos, Thika and Narok Meteorological Stations. The data obtained from these meteorological stations was for periods between five years and thirteen years as shown in the Table 3.1 outlined below;

**Table 3.1; Periods of data Available in Years**

<b>PERIOD OF DATA USED</b>	
<b>STATIONS</b>	<b>Period of Data (Years)</b>
KABETE	From 1995 to 2000
JKIA	From 1995 to 2000, From 2005 to 2010
WILSON	From 1995 to 2000, From 2005 to 2010
DAGORETTI	From 1995 to 2000, From 2005 to 2010
EASTLEIGH	From 1995 to 2003
MACHAKOS	From 1995 to 2000
THIKA	From 1995 to 2000
NAROK	From 1995 to 2000

As seen from Table 3.1, the following wind speed data were not used in the analysis since the data was not available:

- Between the years 2001-2004 for the following stations: JKIA, Wilson and Dagoretti
- After the year 2000 for Kabete, Machakos, Thika and Narok
- After the year 2003 for Eastleigh.

The raw wind speed values obtained were then scanned for statistical outliers. An outlier is a wind speed which is three times greater than both the previous and post hourly (mean) recording (wind speeds such as these would be attributed to local thunderstorm behaviour).

These outliers were removed from subsequent analysis

The hourly mean speeds that were obtained from KMD were in units of knots (nautical mile per hour) and they had been obtained at two different heights i.e. in some stations wind speed measurements were done at 2m height while in others it was done at 10m height. The wind speeds had also been obtained at different terrain (ground roughness) and at anemometers stationed at different heights above the mean sea level. Therefore, before extreme wind



The wind speed (having been already converted to m/s) were then subjected to equation 23 above to get the wind speeds at 10m height.

### **3.2 Determination of Exposure Corrections.**

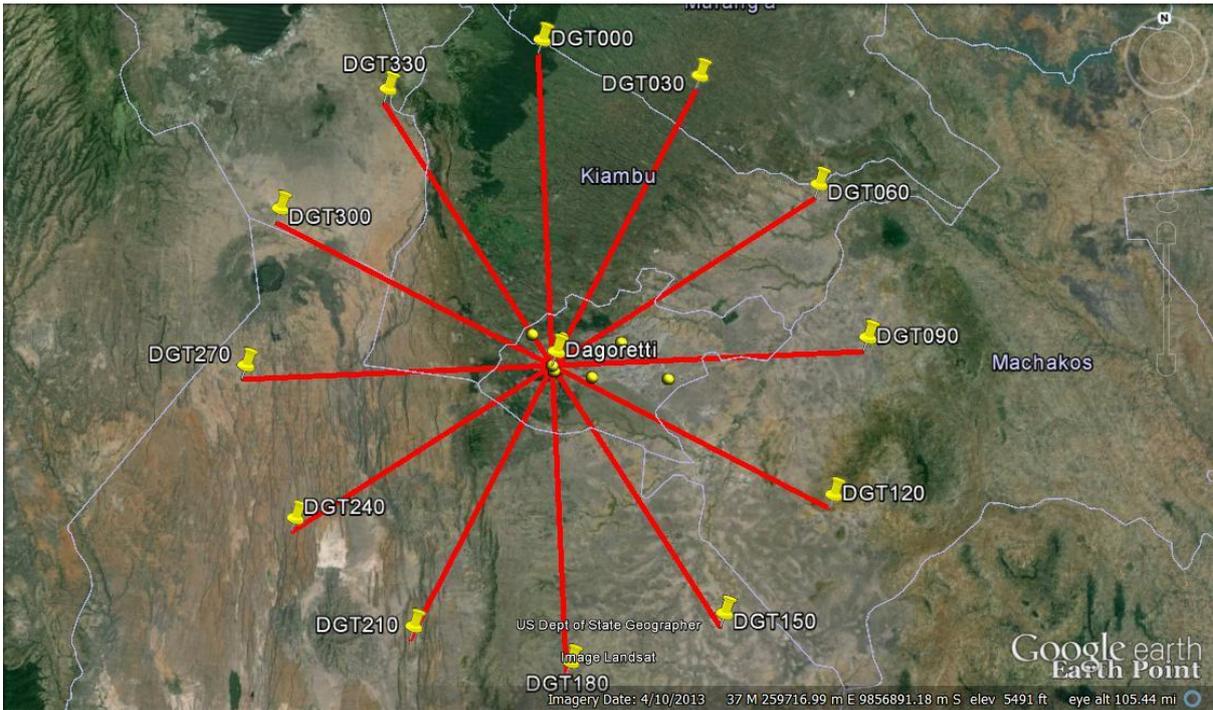
This involved correcting the wind speeds for terrain and altitude so as to obtain the wind speed values at standard terrain i.e. at an area with low vegetation such as grass and isolated obstacles (trees, buildings) with separations of at least 20 obstacle heights ( $Z_0 = 0.05\text{m}$ ) and at the standard altitude which is the mean sea level.

#### **3.2.1 Determination of Terrain Factors**

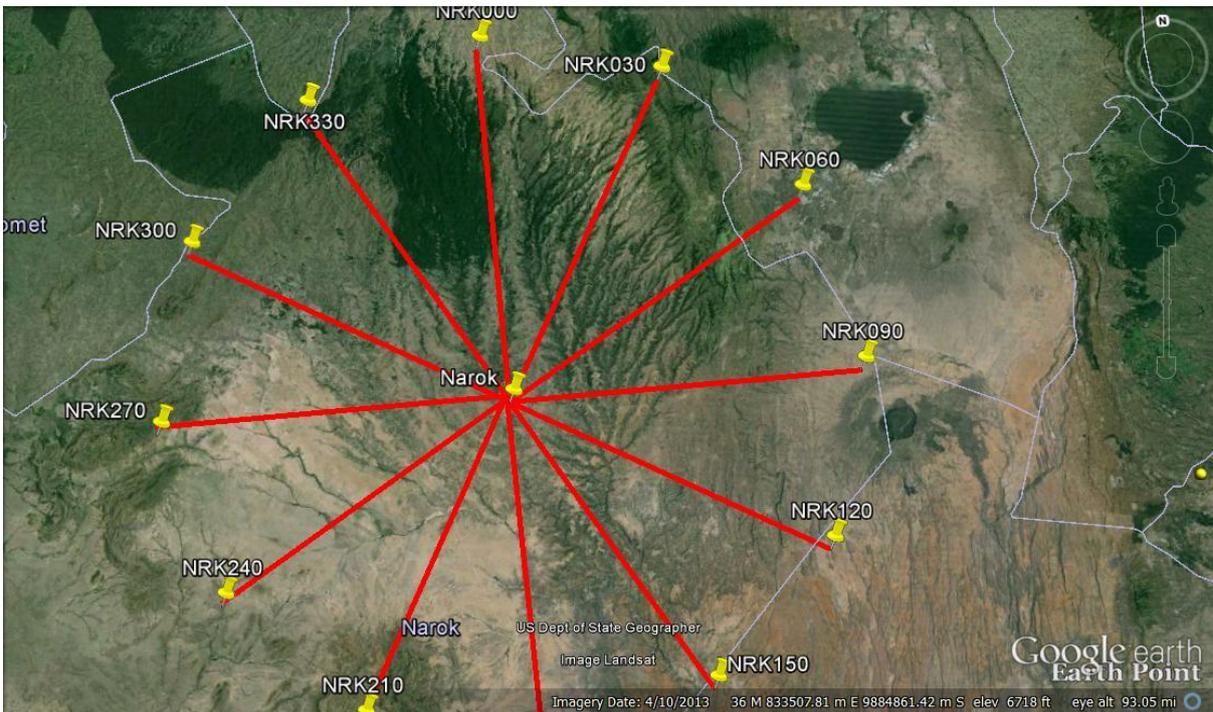
The atmospheric boundary layer model used in the ESDU (Engineering Sciences Data Unit) analysis was used for this analysis. It was developed by Deaves and Harris and takes account of varying surface roughness with fetch. Surface roughness length is characterised by a typical  $Z_0$ , consistent with the model used in ESDU. This method takes into consideration the varying terrain roughness with fetch at 30 degree sectors about the origin of the anemometer. A survey of terrain roughness was carried out for each anemometer using satellite images from the **GOOGLE EARTH** software.

The survey was carried out for a distance of 50km in each direction from the anemometer location. This analysis was carried out for twelve sectors of wind direction from the meteorological station. For each sector, a typical roughness coefficient,  $Z_0$ , was assigned as per Table 2.1 containing the values for typical surface roughness parameter,  $Z_0$ . A conservative assessment of the terrain was made. This conservative estimate considered a rougher upwind thereby resulting in higher factors being applied to the wind records.

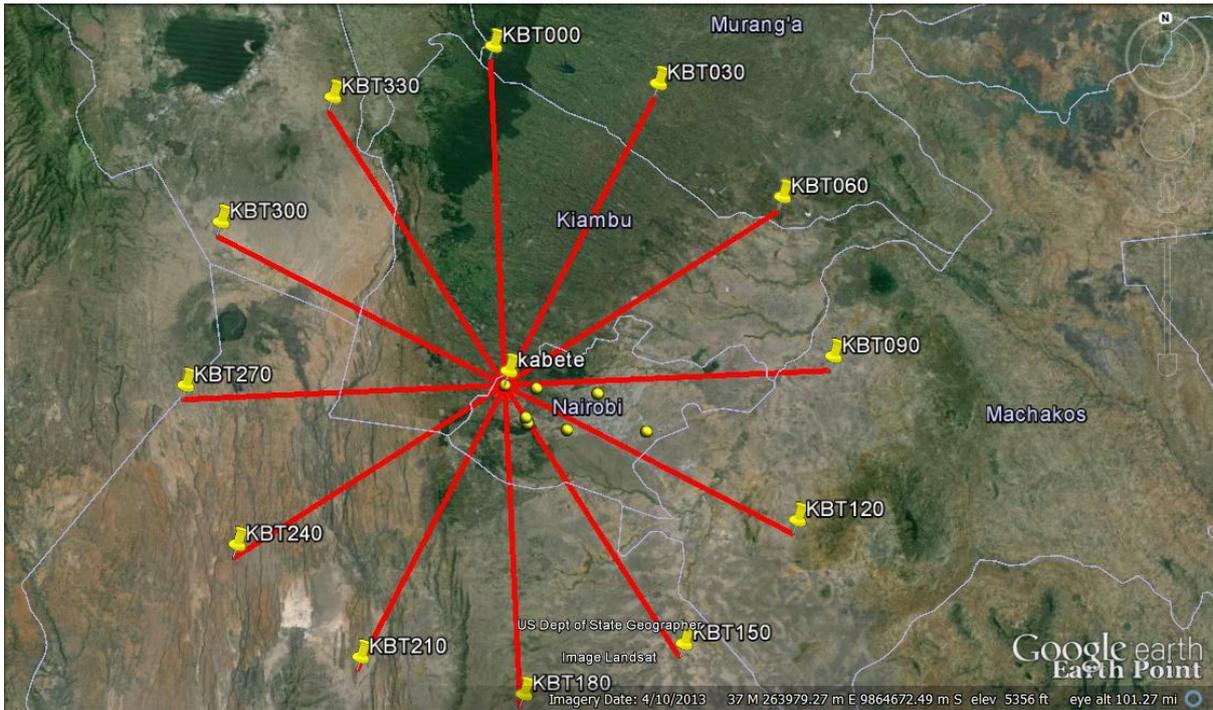
Figures 3.1, 3.2 and 3.3 show the Google earth images which were used in determining the terrain correction factors at Dagoretti, Narok and Kabete meteorological stations respectively



**Figure 3.1. Google Earth Map of Terrain around Dagoretti Meteorological Station**



**Figure 3.2 Google Earth Map of Terrain around Narok Meteorological Station**



**Figure 3.3. Google Earth Map of Terrain around Kabete Agro- Meteorological Station**

### 3.2.2 Determination of Altitude Factors

Design wind speed is usually defined at an elevation of reference that is taken to be the mean sea level. Wind speeds measured at all the anemometers were transposed to the reference altitude which is the mean sea level. The elevations above sea level for each anemometer were obtained from the Kenya Meteorology Department. Based on these elevations, correction factors known as altitude factor ( $S_A$ ) were estimated as recommended in International Standards and used in the Euro code.

The altitude factors were got from the following formulae as given in the United Kingdom National Annex to EN 1991-1-4:

$$S_A = 1 + 0.001(A) \dots \dots \dots \text{Equation 24}$$

Where:  $S_A$  is the Altitude Correction Factor

A is the Altitude in metres.





## DAGORETTI METEOROLOGICAL STATION

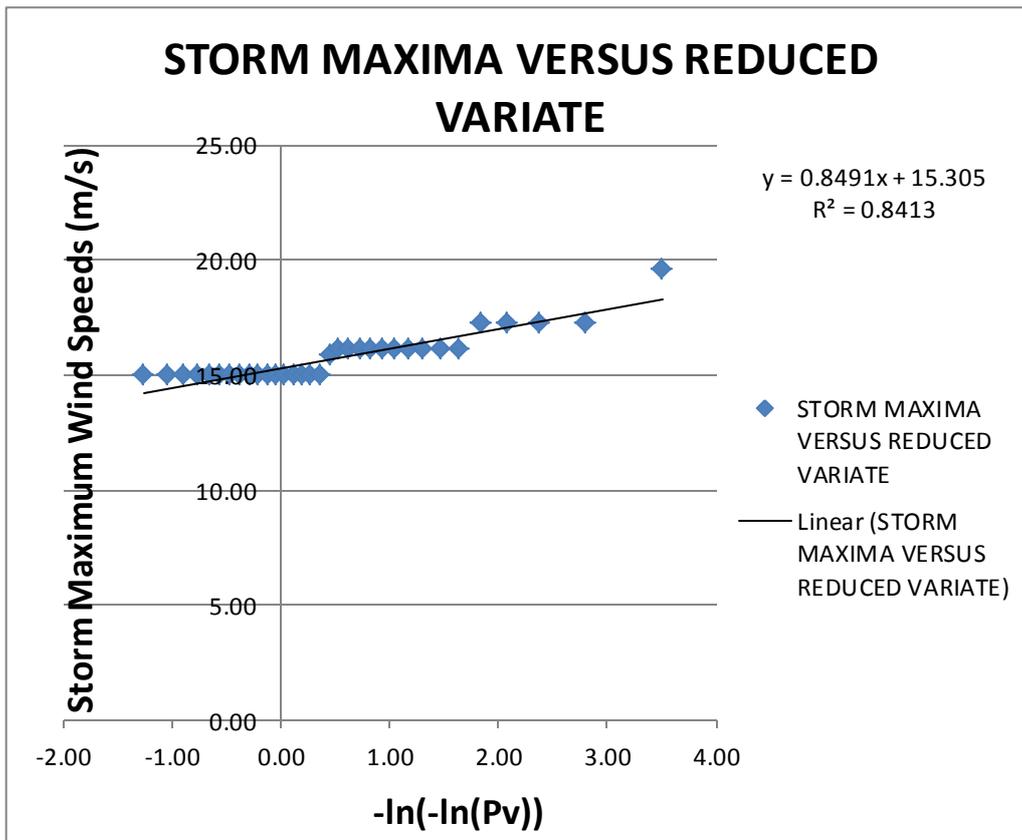
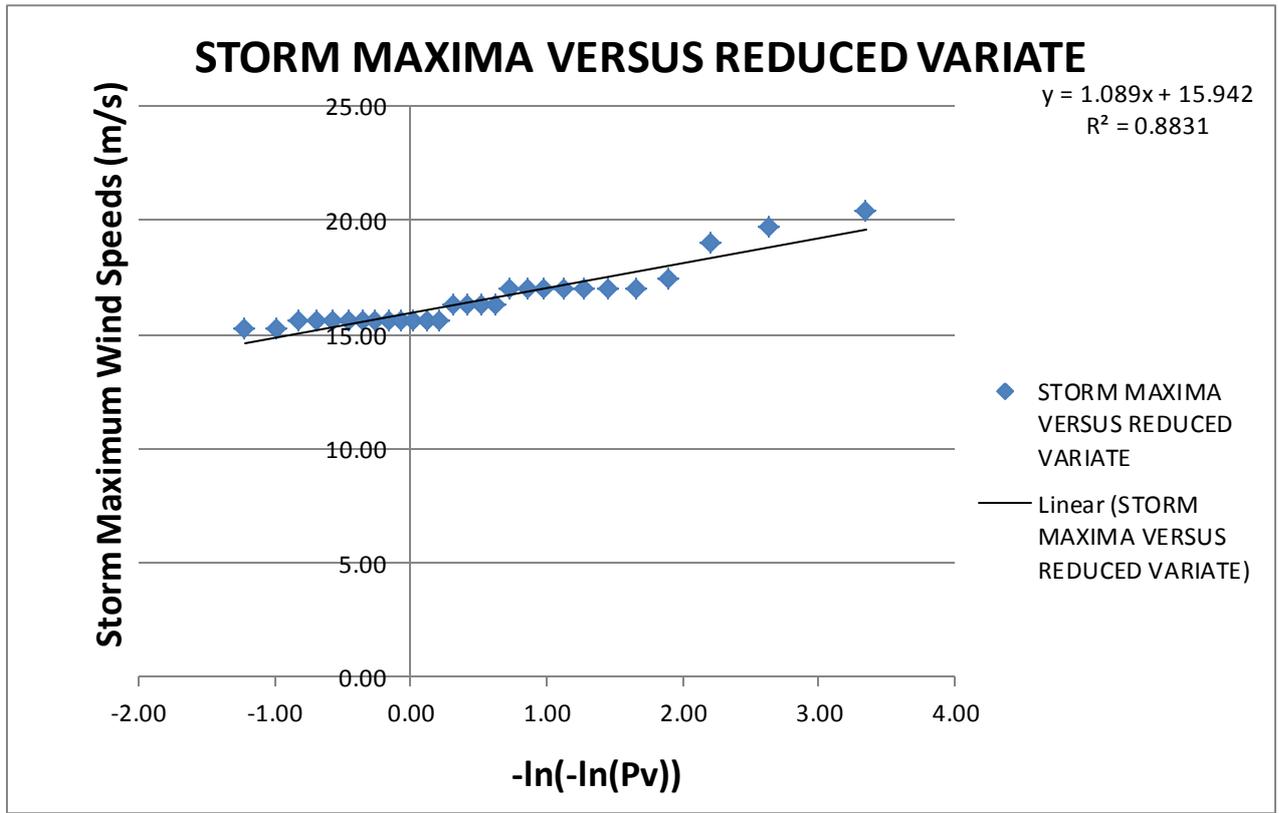


Figure 3.4: Graph of Storm Maximum Wind Speed Versus Reduced variate of Dagoretti Hourly Wind Speeds

## EASTLEIGH METEOROLOGICAL STATION



**Figure 3.5: Graph of Storm Maximum Wind Speed Versus Reduced variate of Eastleigh Hourly Wind Speeds**

# JKIA METEOROLOGICAL STATION

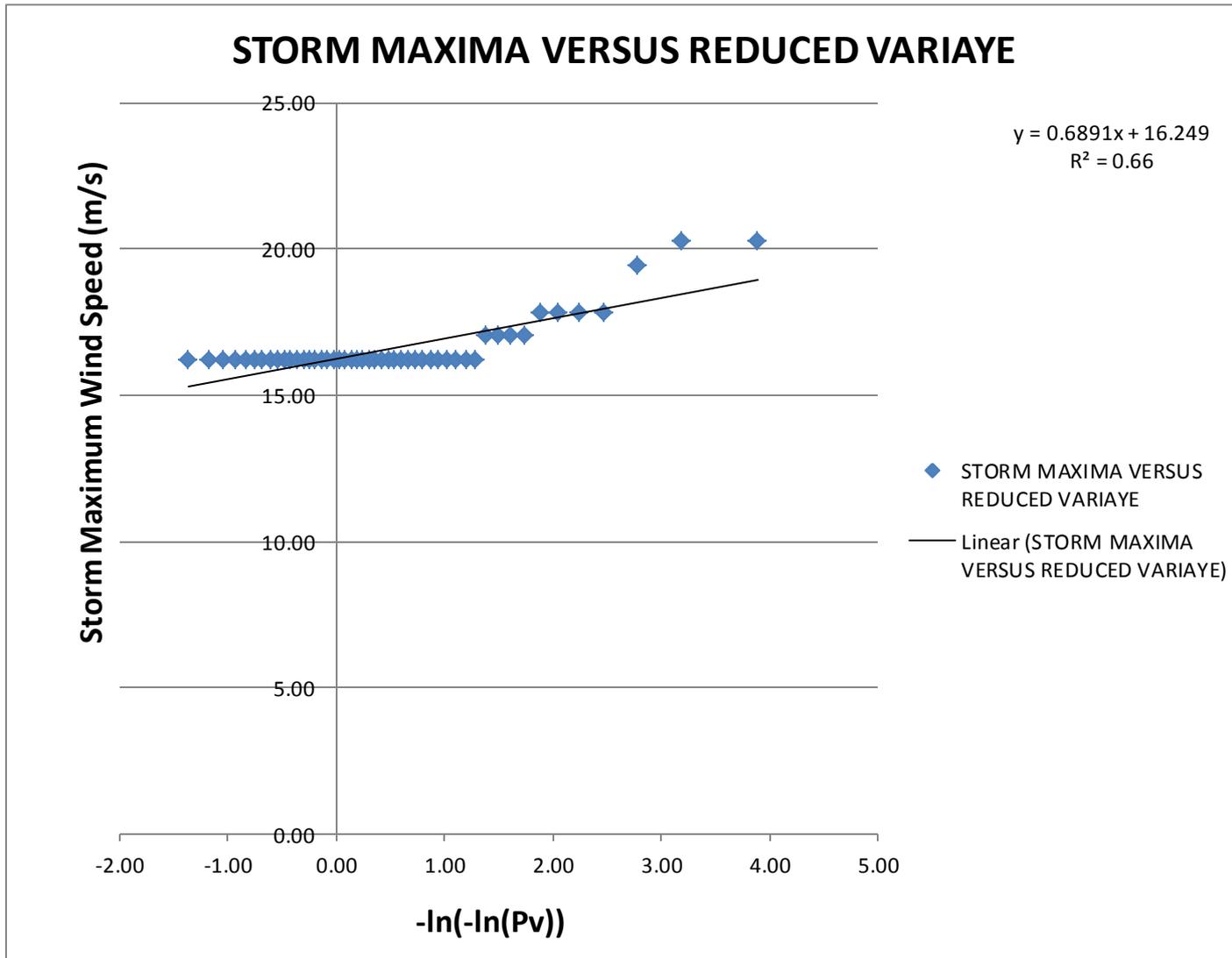


Figure 3.6: Graph of Storm Maximum Wind Speed Versus Reduced variate of JKIA

Hourly Wind Speeds

### KABETE METEOROLOGICAL STATION

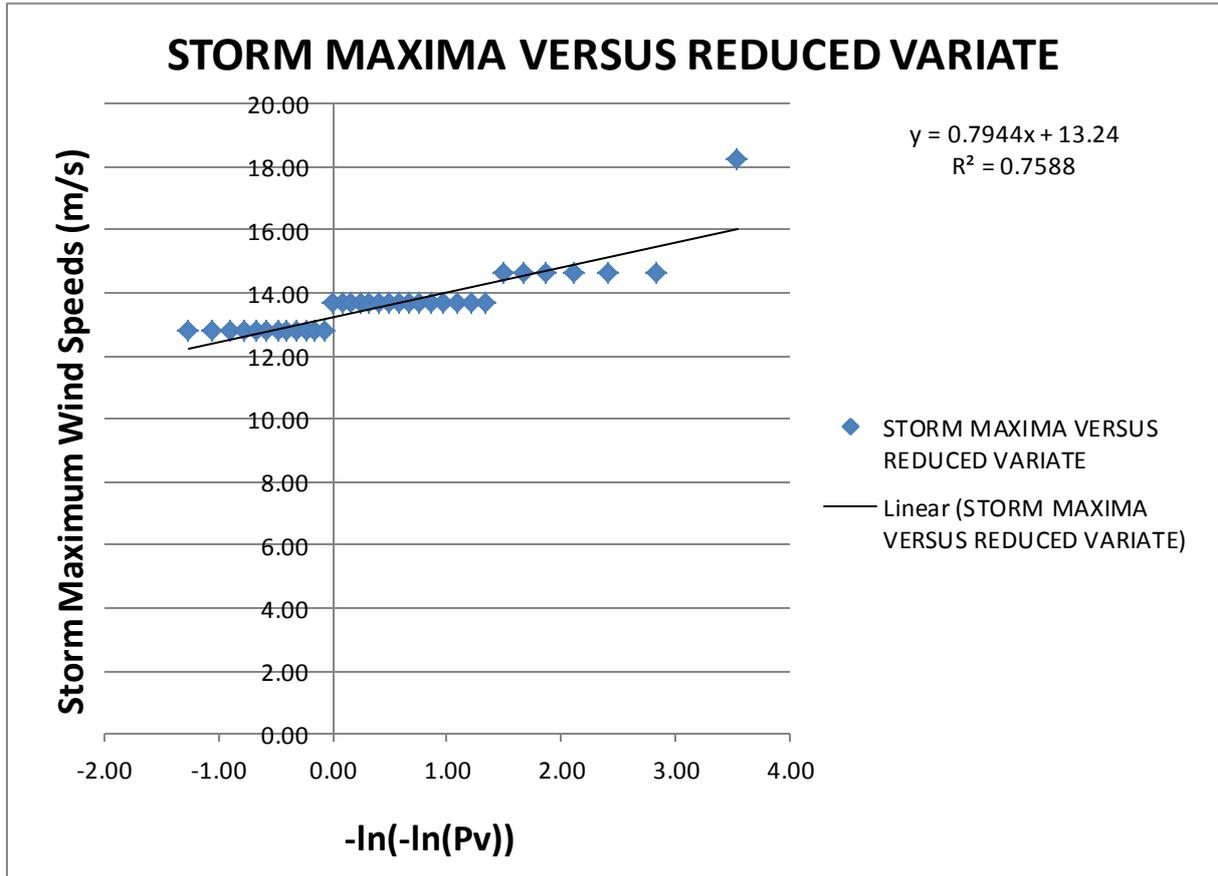


Figure 3.7: Graph of Storm Maximum Wind Speed Versus Reduced variate of Kabete Hourly Wind Speeds

MACHAKOS METEOROLOGICAL STATION

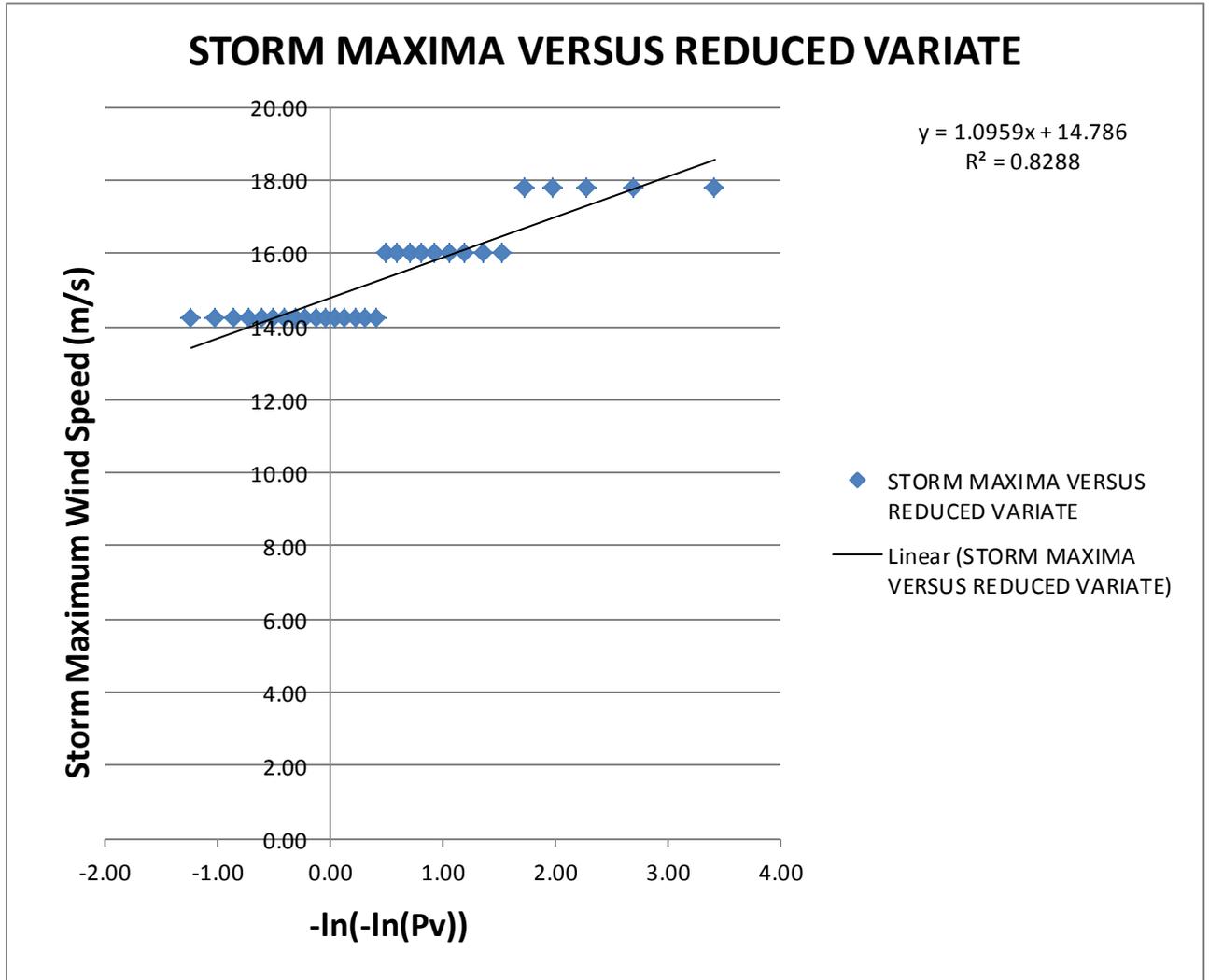
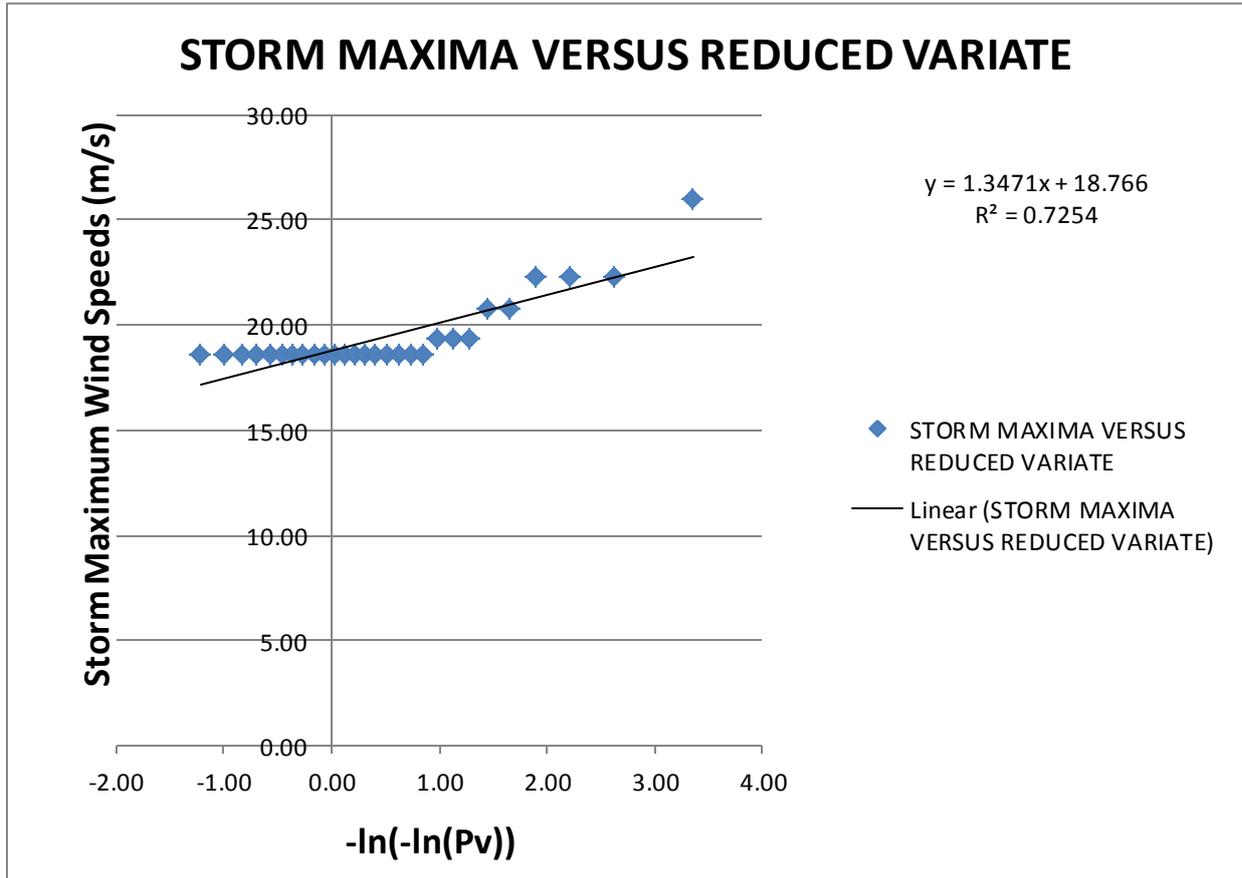


Figure 3.8: Graph of Storm Maximum Wind Speed Versus Reduced variate of Machakos Hourly Wind Speeds

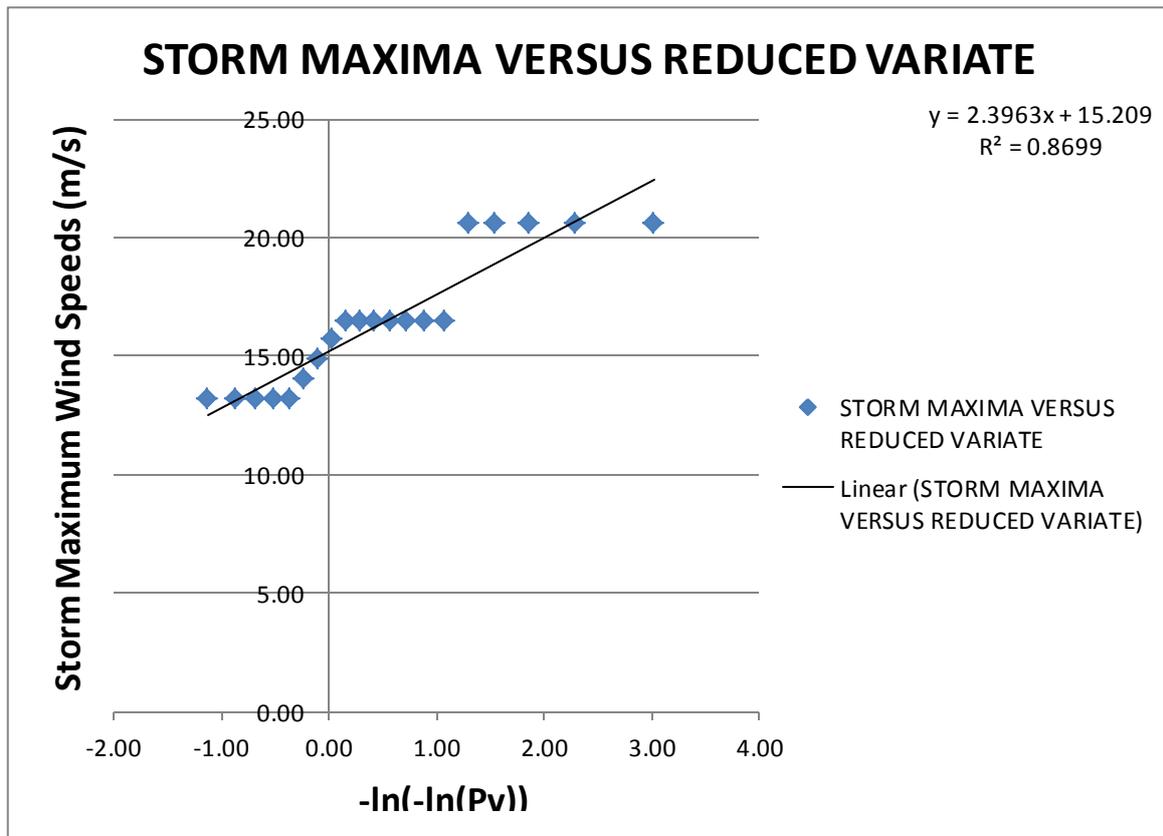
### NAROK METEOROLOGICAL STATION



**Figure 3.9: Graph of Storm Maximum Wind Speed Versus Reduced variate of Narok Hourly Wind Speeds**

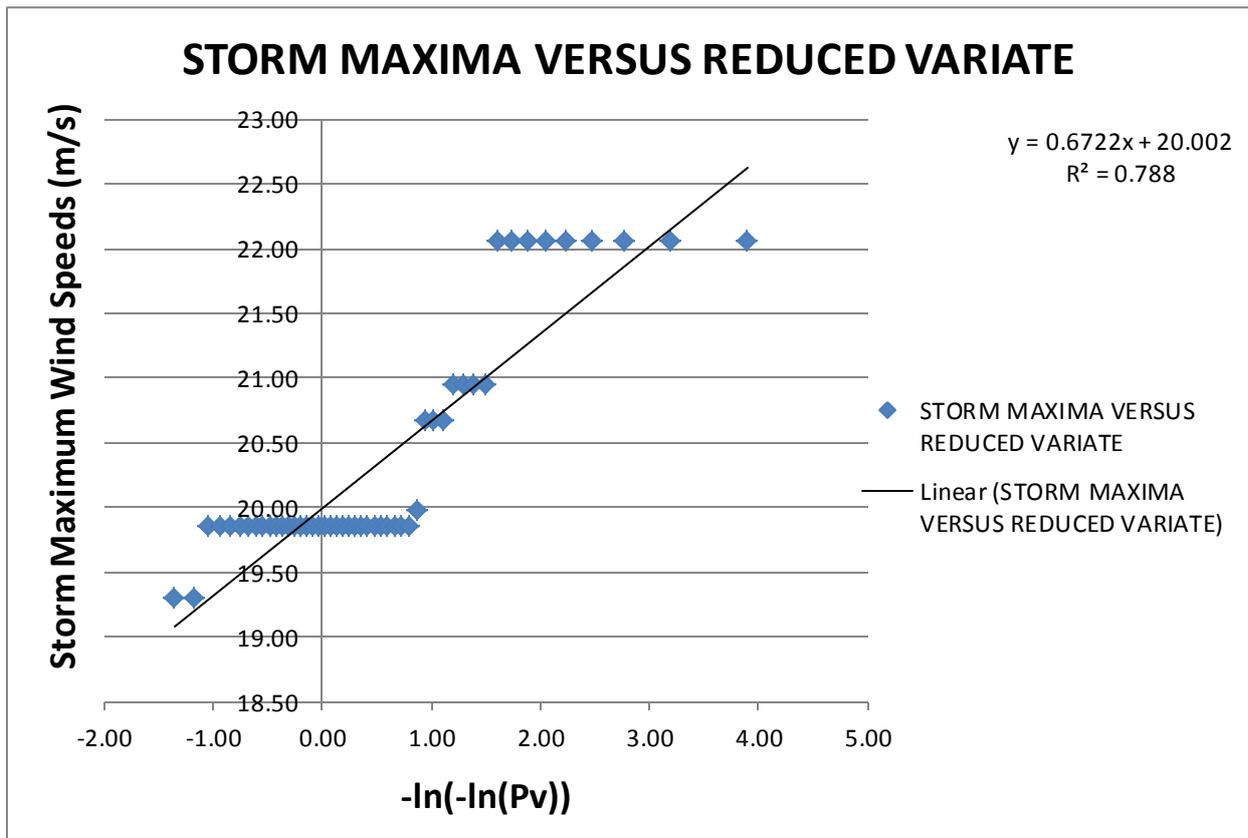


## THIKA METEOROLOGICAL STATION



**Figure 3.10: Graph of Storm Maximum Wind Speed Versus Reduced variate of Thika Hourly Wind Speeds**

## WILSON METEOROLOGICAL STATION



**Figure 3.11: Graph of Storm Maximum Wind Speed Versus Reduced variate of Wilson Airport Hourly Wind Speeds**

### 3.4 Drawing the Wind Speed Map

After obtaining the fundamental basic wind speeds at the meteorological stations, isotachs were drawn on the Nairobi County map. The isotachs were drawn using the NOVAPOINT software. The grid points (latitudes and longitudes) and the fundamental basic wind speeds of each of the meteorological stations were input into the software for it to generate the isotachs. The software was also instructed to generate the isotachs at an interval of 1 m/s. A map of Nairobi County was superimposed on the NOVAPOINT map to ensure that the isotachs map generated would show the boundary of Nairobi County.

## CHAPTER 4: RESULTS AND DISCUSSION

### 4.1 Correction Factors.

These were parameters which were used to transpose the wind speeds measured at the anemometers to a reference terrain and elevation at standard height. They included the terrain correction factors and the altitude correction factors.

#### 4.1.1 Altitude Correction Factors.

The altitude correction factors are the correction factors which transpose the recorded wind speeds to a standard height which is the mean sea level. Nairobi County and its environs generally lie in a high altitude area. Equation 17 shows that the altitude correction factors are directly proportional to the altitude therefore the altitude correction factors were high i.e. Between 2.55 at Thika and 2.89 at Narok.

From Table 4.1 all the altitude correction factor values obtained were greater than one. When these correction factors were multiplied by the raw wind speeds, the resulting wind speed at the mean sea level were higher than the wind speeds measured at the anemometers. This shows that transposition of wind speeds from a high altitude to a lower altitude results in higher wind speeds at the lower altitude. Therefore the wind speeds when transposed to the mean sea level would be higher if only the altitude correction factors were considered. Table 4.1 shows the altitude correction factors that were determined.

**Table 4.1: Altitude Correction Factors.**

**ALTITUDE FACTORS**

STATIONS	ALTITUDE	FACTORS
KABETE	1820	2.82
JKIA	1624	2.62
WILSON	1679	2.68
DAGORETTI	1798	2.80
EASTLEIGH	1640	2.64
MACHAKOS	1750	2.75
THIKA	1549	2.55
NAROK	1890	2.89

**4.1.2 Terrain Correction Factors**

The terrain correction factors are correction factors which transpose the recorded wind speed to the reference terrain which in this case was an area with low vegetation such as grass and isolated obstacles (trees, buildings) with separations of at least 20 obstacle heights ( $Z_0 = 0.05\text{m}$ ). From Table 4.2 the correction factors obtained were all less than one. When these correction factors were multiplied by the raw wind speeds, the resulting wind speed at the reference terrain were lower than the wind speeds measured at the anemometers. This shows that transposition of wind speeds from a rougher terrain (as seen around Nairobi County) to a smoother terrain results in lower wind speeds at the smoother terrain. Therefore the wind speeds when transposed to the reference terrain would be lower if only the terrain correction factors were considered. Table 4.2 shows the terrain correction factors that were determined.

**Table 4.2: Terrain correction factors.**

<b>TERRAIN FACTORS</b>												
<b>STATIONS</b>	<b>DIRECTION IN DEGREES</b>											
	<b>30</b>	<b>60</b>	<b>90</b>	<b>120</b>	<b>150</b>	<b>180</b>	<b>210</b>	<b>240</b>	<b>270</b>	<b>300</b>	<b>330</b>	<b>360</b>
<b>KABETE</b>	0.5	0.5	0.5	0.8	0.4	0.5	0.5	0.5	0.5	0.5	0.5	0.5
<b>JKIA</b>	0.4	0.4	0.3	0.3	0.3	0.3	0.3	0.3	0.5	0.8	0.8	0.6
<b>WILSON</b>	0.8	0.8	0.4	0.3	0.3	0.3	0.3	0.5	0.5	0.5	0.5	0.5
<b>DAGORETTI</b>	0.5	0.5	0.8	0.4	0.3	0.5	0.5	0.5	0.5	0.5	0.5	0.5
<b>EASTLEIGH</b>	0.5	0.4	0.4	0.4	0.4	0.4	0.5	0.5	0.5	0.5	0.5	0.5
<b>MACHAKOS</b>	0.5	0.5	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.5	0.5
<b>THIKA</b>	0.5	0.5	0.5	0.5	0.4	0.3	0.3	0.3	0.5	0.5	0.5	0.5
<b>NAROK</b>	0.5	0.5	0.5	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.5	0.5

#### **4.1.3 Combined Correction Factors**

The altitude correction factors were multiplied by the terrain correction factors to result in the combined correction factors. The combined correction factors show the overall effect of the correction factors on the wind speed measurements. If the combined correction factors are greater than one, then the wind speeds at the reference terrain and altitude would be higher than the wind speeds measured at the anemometers. However, if the combined correction factors are less than one, then the wind speeds at the reference terrain and altitude would be lower than the wind speeds measured at the anemometers.

From Table 4.3 showing the correction factors obtained, 69.79% of the values were greater than one while 30.21% of them were less than one. Therefore, generally in Nairobi County, the wind speeds at the reference terrain and elevation were greater than the measured wind speeds. Therefore from the combined correction factors, it is seen that if the extreme wind

analysis is carried out without considering the correction factors then the resulting fundamental basic wind speeds would be lower than they really are. Table 4.3 shows the combined correction factors.

**Table 4.3: Combined Correction Factors.**

STATIONS	WIND DIRECTION											
	30	60	90	120	150	180	210	240	270	300	330	360
<b>KABETE</b>	1.41	1.41	1.41	2.26	1.13	1.41	1.41	1.41	1.41	1.41	1.41	1.41
<b>JKIA</b>	1.05	1.05	0.79	0.79	0.79	0.79	0.79	0.79	1.31	2.10	2.10	1.57
<b>WILSON</b>	2.14	2.14	1.07	0.80	0.80	0.80	0.80	1.34	1.34	1.34	1.34	1.34
<b>DAGORETTI</b>	1.40	1.40	2.24	1.12	0.84	1.40	1.40	1.40	1.40	1.40	1.40	1.40
<b>EASTLEIGH</b>	1.32	1.06	1.06	1.06	1.06	1.06	1.32	1.32	1.32	1.32	1.32	1.32
<b>MACHAKOS</b>	1.38	1.38	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.83	1.38	1.38
<b>THIKA</b>	1.27	1.27	1.27	1.27	1.02	0.76	0.76	0.76	1.27	1.27	1.27	1.27
<b>NAROK</b>	1.45	1.45	1.45	0.87	0.87	0.87	0.87	0.87	0.87	0.87	1.45	1.45

### 4.3 Basic Mean Hourly Wind Speeds.

The basic mean hourly wind speeds are the wind speeds that resulted from the extreme value analysis of the hourly wind speeds that had been transposed to reference terrain and elevation at standard height. The analysis is shown in Tables A1 to A8 in appendix A. Table 4.4 shows

the basic mean hourly wind speeds in Nairobi County and its environs. The wind speeds vary from 16.34m/s at Kabete to 24.56m/s at Thika. Previously, the 3-second gust speeds in Nairobi County has been assumed to be 28m/s. From the durst curve in figure 2.1, the conversion factor from a mean hourly wind speed to a 3-second gust speed is 1.52. The mean hourly wind speed is obtained by dividing 28m/s by 1.52. Therefore this translates to a mean hourly wind speed of 18.42m/s which is comparable to the wind speeds obtained from the analysis.

**Table 4.4: Basic Mean Hourly Design Speeds**

<b>STATIONS</b>	<b>Basic Hourly Mean Design Speed(m/s)</b>
KABETE	16.34
JKIA	18.94
WILSON	22.62
DAGORETTI	18.62
EASTLEIGH	20.19
MACHAKOS	19.06
THIKA	24.56
NAROK	24.02

#### **4.4 Basic 10 Minute Wind Speeds.**

EN 1991-1-4 defines the fundamental basic wind speed in form of a 10-minute speed. Thus it proposes an averaging period of 10 minute. Therefore the mean hourly wind speeds obtained in Table 4.4 were multiplied by a factor 1.06 got from Figure 2.1. to obtain the 10-minute wind speeds shown in Table 4.5 below. From Table 4.5, the 10-minute wind speed varies from 17.32m/s to 26.03m/s. When the 3 second gust speed currently in use in Nairobi County

is converted to a mean hourly wind speed using the durst curve from figure 2.1, it results in a mean hourly wind speed of 18.52m/s. When this wind speed is multiplied by the factor from figure 2.1 which is 1.06, a 10 minute wind speed of 19.63m/s is obtained. This is comparable with the 10 minute

**Table 4.5: 10-Minute Design Wind Speed**

<b>STATIONS</b>	<b>Basic 10-min Design Speed(m/s)</b>
KABETE	17.32
JKIA	20.08
WILSON	23.98
DAGORETTI	19.74
EASTLEIGH	21.40
MACHAKOS	20.20
THIKA	26.03
NAROK	25.46

#### **4.5 Nairobi County Wind Speed Map**

From the 10 minute wind speeds in Table 4.5, the Nairobi County wind speed map shown in Figure 4.1 was drawn. This map was drawn using software known as NOVAPOINT. To draw the map the 10 minute basic wind speeds and the grid points (longitudes and latitudes) of each of the meteorological stations were input into the software. The isotachs were drawn at an interval of 1m/s. From the wind speed map in Figure 4.1, the 10 minute wind speeds within Nairobi County vary from 18m/s to 22m/s. This is comparable to 19.63m/s which is what would have been obtained if the 3-second wind speed currently in use i.e. 28m/s would have been converted to a 10 minute wind speed using the durst curve from Figure 2.1.

It is important to note that the wind speed of short recording time is usually higher than the wind speed of long recording time. Therefore it is most probable that the wind speeds obtained from this research were affected by the period of data available. The data available ranged from 6 years to 12 years. This could have resulted in higher wind speeds. Longer recording periods would have led to more accurate results.

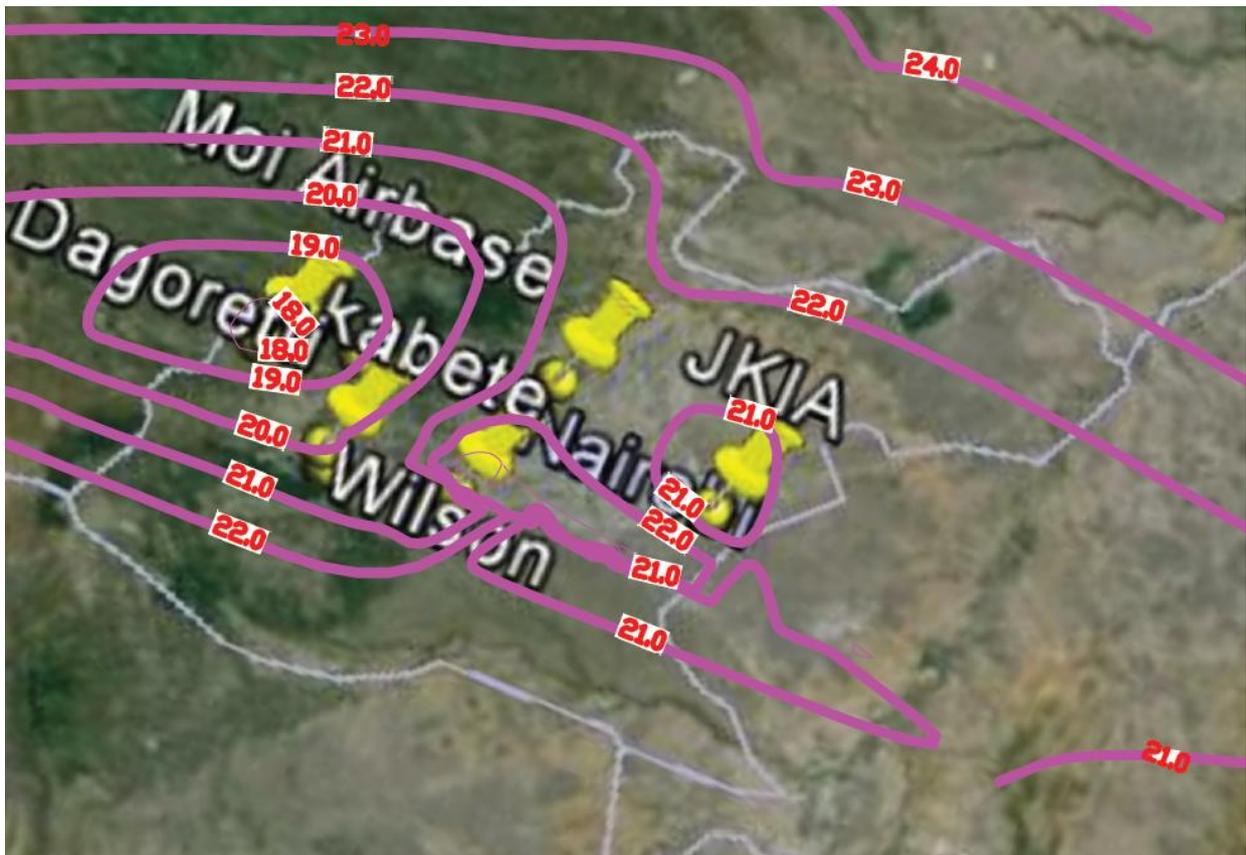


Figure 4.1: Nairobi Wind map

## **CHAPTER 5: CONCLUSIONS AND RECOMMENDATIONS**

### **5.1. CONCLUSION**

1. This research has led to the development of a Nairobi County wind speed map which can be used to determine wind loads on various structures within Nairobi County. The contour map obtained can be used with Euro code 1991-1-4 since it is based on 10-min mean wind speed at sea level ( $Z_0 = 0.03\text{m}$ ) which has a probability of 0.02 of being exceeded in any one year.
2. The basic 10 minute mean wind speeds within Nairobi County vary from 18m/s to 22m/s.
3. The current basic 3-second gust speed used in Nairobi County is 28m/s. When converted to a 10 minute wind speed, it becomes 19.63m/s which is within the range of basic wind speeds obtained for Nairobi County.

### **5.2 RECOMMENDATIONS.**

1. The Nairobi County Contour wind map obtained from this research should be used alongside the Euro code 1991-1-4 in determination of wind loads in Nairobi County.
2. Future research should cover the whole country so as to result in a National Wind Map.
3. Kenya Meteorological Department (KMD) should strive to have and avail hourly wind speeds for all the meteorological stations in Kenya to ensure research covering the whole country can be successfully carried out.
4. Kenya Meteorological Department (KMD) should strive to have and avail hourly wind speeds covering longer periods i.e. over 20 years since it will lead to higher accuracy of the results.

5. Kenya Meteorological Department should employ Automatic Weather Station (AWS) technology as this increase the wind data available for extreme wind analysis since more accurate data from many other locations apart from the meteorological stations can be got.

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## APPENDIX A

**Table A.1: Table of Analysis of Dagoretti Independent Storm Maximum Wind Speeds**

DAGORETTI WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
14.97	1	33	0.03	3.53	-1.26
14.97	2	33	0.06	2.83	-1.04
14.97	3	33	0.09	2.43	-0.89
14.97	4	33	0.12	2.14	-0.76
14.97	5	33	0.15	1.92	-0.65
14.97	6	33	0.18	1.73	-0.55
14.97	7	33	0.21	1.58	-0.46
14.97	8	33	0.24	1.45	-0.37
14.97	9	33	0.26	1.33	-0.28
14.97	10	33	0.29	1.22	-0.20
14.97	11	33	0.32	1.13	-0.12
14.97	12	33	0.35	1.04	-0.04
14.97	13	33	0.38	0.96	0.04
14.97	14	33	0.41	0.89	0.12
14.97	15	33	0.44	0.82	0.20
14.97	16	33	0.47	0.75	0.28
14.97	17	33	0.50	0.69	0.37
15.83	18	33	0.53	0.64	0.45
16.12	19	33	0.56	0.58	0.54
16.12	20	33	0.59	0.53	0.63
16.12	21	33	0.62	0.48	0.73
16.12	22	33	0.65	0.44	0.83
16.12	23	33	0.68	0.39	0.94
16.12	24	33	0.71	0.35	1.05
16.12	25	33	0.74	0.31	1.18
16.12	26	33	0.76	0.27	1.32
16.12	27	33	0.79	0.23	1.47
16.12	28	33	0.82	0.19	1.64
17.27	29	33	0.85	0.16	1.84
17.27	30	33	0.88	0.13	2.08
17.27	31	33	0.91	0.09	2.38
17.27	32	33	0.94	0.06	2.80
19.57	33	33	0.97	0.03	3.51

**Table A.2: Table of Analysis of Eastleigh Independent Storm Maximum Wind Speeds**

<b>EASTLEIGH WIND ANALYSIS</b>					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
15.21	1	28	0.03	3.37	-1.21
15.21	2	28	0.07	2.67	-0.98
15.62	3	28	0.10	2.27	-0.82
15.62	4	28	0.14	1.98	-0.68
15.62	5	28	0.17	1.76	-0.56
15.62	6	28	0.21	1.58	-0.45
15.62	7	28	0.24	1.42	-0.35
15.62	8	28	0.28	1.29	-0.25
15.62	9	28	0.31	1.17	-0.16
15.62	10	28	0.34	1.06	-0.06
15.62	11	28	0.38	0.97	0.03
15.62	12	28	0.41	0.88	0.13
15.62	13	28	0.45	0.80	0.22
16.30	14	28	0.48	0.73	0.32
16.30	15	28	0.52	0.66	0.42
16.30	16	28	0.55	0.59	0.52
16.30	17	28	0.59	0.53	0.63
16.98	18	28	0.62	0.48	0.74
16.98	19	28	0.66	0.42	0.86
16.98	20	28	0.69	0.37	0.99
16.98	21	28	0.72	0.32	1.13
16.98	22	28	0.76	0.28	1.29
16.98	23	28	0.79	0.23	1.46
16.98	24	28	0.83	0.19	1.66
17.38	25	28	0.86	0.15	1.91
19.01	26	28	0.90	0.11	2.21
19.69	27	28	0.93	0.07	2.64
20.37	28	28	0.97	0.04	3.35

**Table A.3: Table of Analysis of JKIA Independent Storm Maximum Wind Speeds**

JKIA WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
16.20	1	35	0.02	3.91	-1.36
16.20	2	35	0.04	3.22	-1.17
16.20	3	35	0.06	2.81	-1.03
16.20	4	35	0.08	2.53	-0.93
16.20	5	35	0.10	2.30	-0.83
16.20	6	35	0.40	0.92	0.09
16.20	7	35	0.42	0.87	0.14
16.20	8	35	0.44	0.82	0.20
16.20	9	35	0.46	0.78	0.25
16.20	10	35	0.48	0.73	0.31
16.20	11	35	0.50	0.69	0.37
16.20	12	35	0.52	0.65	0.42
16.20	13	35	0.54	0.62	0.48
16.20	14	35	0.56	0.58	0.55
16.20	15	35	0.58	0.54	0.61
16.20	16	35	0.60	0.51	0.67
16.20	17	35	0.62	0.48	0.74
16.20	18	35	0.64	0.45	0.81
16.20	19	35	0.66	0.42	0.88
16.20	20	35	0.68	0.39	0.95
16.20	21	35	0.70	0.36	1.03
16.20	22	35	0.72	0.33	1.11
16.20	23	35	0.74	0.30	1.20
16.20	24	35	0.76	0.27	1.29
17.01	25	35	0.78	0.25	1.39
17.01	26	35	0.80	0.22	1.50
17.01	27	35	0.82	0.20	1.62
17.01	28	35	0.84	0.17	1.75
17.82	29	35	0.86	0.15	1.89
17.82	30	35	0.88	0.13	2.06
17.82	31	35	0.90	0.11	2.25
17.82	32	35	0.92	0.08	2.48
19.44	33	35	0.94	0.06	2.78
20.25	34	35	0.96	0.04	3.20
20.25	35	35	0.98	0.02	3.90

**Table A.4: Table of Analysis of Kabete Independent Storm Maximum Wind Speeds**

KABETE WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
12.78	1	34	0.03	3.56	-1.27
12.78	2	34	0.06	2.86	-1.05
12.78	3	34	0.09	2.46	-0.90
12.78	4	34	0.11	2.17	-0.77
12.78	5	34	0.14	1.95	-0.67
12.78	6	34	0.17	1.76	-0.57
12.78	7	34	0.20	1.61	-0.48
12.78	8	34	0.23	1.48	-0.39
12.78	9	34	0.26	1.36	-0.31
12.78	10	34	0.29	1.25	-0.23
12.78	11	34	0.31	1.16	-0.15
12.78	12	34	0.34	1.07	-0.07
13.70	13	34	0.37	0.99	0.01
13.70	14	34	0.40	0.92	0.09
13.70	15	34	0.43	0.85	0.17
13.70	16	34	0.46	0.78	0.24
13.70	17	34	0.49	0.72	0.33
13.70	18	34	0.51	0.66	0.41
13.70	19	34	0.54	0.61	0.49
13.70	20	34	0.57	0.56	0.58
13.70	21	34	0.60	0.51	0.67
13.70	22	34	0.63	0.46	0.77
13.70	23	34	0.66	0.42	0.87
13.70	24	34	0.69	0.38	0.97
13.70	25	34	0.71	0.34	1.09
13.70	26	34	0.74	0.30	1.21
13.70	27	34	0.77	0.26	1.35
14.61	28	34	0.80	0.22	1.50
14.61	29	34	0.83	0.19	1.67
14.61	30	34	0.86	0.15	1.87
14.61	31	34	0.89	0.12	2.11
14.61	32	34	0.91	0.09	2.41
14.61	33	34	0.94	0.06	2.83
18.26	34	34	0.97	0.03	3.54

**Table A.5: Table of Analysis of Machakos Independent Storm Maximum Wind Speeds.**

MACHAKOS WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
14.25	1	30	0.03	3.43	-1.23
14.25	2	30	0.06	2.74	-1.01
14.25	3	30	0.10	2.34	-0.85
14.25	4	30	0.13	2.05	-0.72
14.25	5	30	0.16	1.82	-0.60
14.25	6	30	0.19	1.64	-0.50
14.25	7	30	0.23	1.49	-0.40
14.25	8	30	0.26	1.35	-0.30
14.25	9	30	0.29	1.24	-0.21
14.25	10	30	0.32	1.13	-0.12
14.25	11	30	0.35	1.04	-0.04
14.25	12	30	0.39	0.95	0.05
14.25	13	30	0.42	0.87	0.14
14.25	14	30	0.45	0.79	0.23
14.25	15	30	0.48	0.73	0.32
14.25	16	30	0.52	0.66	0.41
16.03	17	30	0.55	0.60	0.51
16.03	18	30	0.58	0.54	0.61
16.03	19	30	0.61	0.49	0.71
16.03	20	30	0.65	0.44	0.82
16.03	21	30	0.68	0.39	0.94
16.03	22	30	0.71	0.34	1.07
16.03	23	30	0.74	0.30	1.21
16.03	24	30	0.77	0.26	1.36
16.03	25	30	0.81	0.22	1.54
17.81	26	30	0.84	0.18	1.74
17.81	27	30	0.87	0.14	1.98
17.81	28	30	0.90	0.10	2.28
17.81	29	30	0.94	0.07	2.71
17.81	30	30	0.97	0.03	3.42

**Table A.6: Table of Analysis of Narok Independent Storm Maximum Wind Speeds.**

NAROK WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
18.58	1	28	0.03	3.37	-1.21
18.58	2	28	0.07	2.67	-0.98
18.58	3	28	0.10	2.27	-0.82
18.58	4	28	0.14	1.98	-0.68
18.58	5	28	0.17	1.76	-0.56
18.58	6	28	0.21	1.58	-0.45
18.58	7	28	0.24	1.42	-0.35
18.58	8	28	0.28	1.29	-0.25
18.58	9	28	0.31	1.17	-0.16
18.58	10	28	0.34	1.06	-0.06
18.58	11	28	0.38	0.97	0.03
18.58	12	28	0.41	0.88	0.13
18.58	13	28	0.45	0.80	0.22
18.58	14	28	0.48	0.73	0.32
18.58	15	28	0.52	0.66	0.42
18.58	16	28	0.55	0.59	0.52
18.58	17	28	0.59	0.53	0.63
18.58	18	28	0.62	0.48	0.74
18.58	19	28	0.66	0.42	0.86
19.33	20	28	0.69	0.37	0.99
19.33	21	28	0.72	0.32	1.13
19.33	22	28	0.76	0.28	1.29
20.81	23	28	0.79	0.23	1.46
20.81	24	28	0.83	0.19	1.66
22.30	25	28	0.86	0.15	1.91
22.30	26	28	0.90	0.11	2.21
22.30	27	28	0.93	0.07	2.64
26.02	28	28	0.97	0.04	3.35

**Table A.7: Table of Analysis of Thika Independent Storm Maximum Wind Speeds.**

THIKA WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
13.20	1	20	0.05	3.04	-1.11
13.20	2	20	0.10	2.35	-0.86
13.20	3	20	0.14	1.95	-0.67
13.20	4	20	0.19	1.66	-0.51
13.20	5	20	0.24	1.44	-0.36
14.03	6	20	0.29	1.25	-0.23
14.85	7	20	0.33	1.10	-0.09
15.68	8	20	0.38	0.97	0.04
16.51	9	20	0.43	0.85	0.17
16.51	10	20	0.48	0.74	0.30
16.51	11	20	0.52	0.65	0.44
16.51	12	20	0.57	0.56	0.58
16.51	13	20	0.62	0.48	0.73
16.51	14	20	0.67	0.41	0.90
16.51	15	20	0.71	0.34	1.09
20.63	16	20	0.76	0.27	1.30
20.63	17	20	0.81	0.21	1.55
20.63	18	20	0.86	0.15	1.87
20.63	19	20	0.90	0.10	2.30
20.63	20	20	0.95	0.05	3.02

**Table A.8: Table of Analysis of Wilson Independent Storm Maximum Wind Speeds.**

WILSON WIND ANALYSIS					
V	m	N	Pv	-ln(Pv)	-ln(-ln(Pv))
19.29	1	35	0.02	3.91	-1.36
19.29	2	35	0.04	3.22	-1.17
19.84	3	35	0.06	2.81	-1.03
19.84	4	35	0.08	2.53	-0.93
19.84	5	35	0.10	2.30	-0.83
19.84	6	35	0.12	2.12	-0.75
19.84	7	35	0.14	1.97	-0.68
19.84	8	35	0.16	1.83	-0.61
19.84	9	35	0.46	0.78	0.25
19.84	10	35	0.48	0.73	0.31
19.84	11	35	0.50	0.69	0.37
19.84	12	35	0.52	0.65	0.42
19.84	13	35	0.54	0.62	0.48
19.84	14	35	0.56	0.58	0.55
19.84	15	35	0.58	0.54	0.61
19.84	16	35	0.60	0.51	0.67
19.84	17	35	0.62	0.48	0.74
19.84	18	35	0.64	0.45	0.81
19.98	19	35	0.66	0.42	0.88
20.67	20	35	0.68	0.39	0.95
20.67	21	35	0.70	0.36	1.03
20.67	22	35	0.72	0.33	1.11
20.95	23	35	0.74	0.30	1.20
20.95	24	35	0.76	0.27	1.29
20.95	25	35	0.78	0.25	1.39
20.95	26	35	0.80	0.22	1.50
22.05	27	35	0.82	0.20	1.62
22.05	28	35	0.84	0.17	1.75
22.05	29	35	0.86	0.15	1.89
22.05	30	35	0.88	0.13	2.06
22.05	31	35	0.90	0.11	2.25
22.05	32	35	0.92	0.08	2.48
22.05	33	35	0.94	0.06	2.78
22.05	34	35	0.96	0.04	3.20
22.05	35	35	0.98	0.02	3.90

